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DIGITAL INTERFERMETRY APPLIED TO THERMOGRAVITATIONAL TECHNIQUE 1

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Abstract 7

- In this work, we have applied Optical Digital
- Interferometry approach
- thermogravitational micro-column 10
- technique. 11
- By the new analysis, we examine the entire 12
- height of the micro-column and determine the 13
- complete concentration profile inside. The
- measurements were carried out by two lasers 15
- with different wavelength $\lambda = 633nm$ and 16
- 17 $\lambda = 470nm$. The system was validated with
- 18 binary subsystems of the THN-IBB-C12
- 19
- ternary mixture at equal mass fractions. The
- 20 results were compared with values of 21 Benchmark Fontainebleau and they showed
- an excellent agreement.
- Thermodiffusion, 23 **Keywords**: binary
- mixtures, Thermogravitational 24 micro-
- column, Optical Digital Interferometry. 25

1. Introduction 26

- Since over last decades, optical methods have 27
- been widely used in the determination of 28
- transport properties as the thermodiffusion, 29
- molecular diffusion and Soret coefficients of
- binary mixtures. For example, Optical Beam
- Deflection (Kolodner et al. 1988; Zhang et al.
- 33 1996), Optical Digital Interferometry
- 34 (Mialdun and Shevtsova 2008) and Thermal
- Diffusion Forced Rayleigh Scattering
- (Wiegand et al. 2007; Wittko and Köhler
- 2003) have been used to analyse several
- binary mixtures. All these optical methods
- have demonstrated good sensitivity in 39
- measurements. 40
- Now the challenge is focused on ternary 41
- mixtures, so many of these techniques have 42
- been modified in order to analyse more

- complex systems. As a result, nowadays
- several instruments such as (Gebhardt et al.
- 2013) and (Mialdun et al. 2015) are able to
- determine the transport properties of different 47
- ternary mixtures using optical analysis
- methods or by samples extraction (Larrañaga 49
- 50 et al. 2015).
- Optical methods allow to work with small 51
- sample volume because the measurements
- are usually carried out in situ. In the case of
- biological substances, for instance, it is not
- 55 always easy or possible to obtain big samples.
- 56 The conventional thermogravitational
- 57 cylindrical columns parallelepiped and
- (Larrañaga et al. 2015b; Urteaga et al. 2012)
- need at least 30 ml of sample, so it is not
- viable to analyse biological samples using
- those techniques. For this reason, a new 61
- 62 thermogravitational micro-column
- 63 designed, constructed and validated in
- 64 Mondragon University (Naumann et
- 65 2012) in order to determine
- thermodiffusion coefficient purely by optical 66
- method. The sample volume of this micro-67
- column is less than 50 µl so it makes feasible 68
- the investigation of expensive substances, 69
- 70 which cannot be obtained in large quantities.
- The optical approach applied to the micro-71
- 72 column, made possible to analyse the
- 73 continuous concentration profile in binary
- 74 mixtures between two points. Nevertheless,
- 75 by this analysis method (Naumann et al.
- 2012), the accuracy of determining the
- 77 vertical concentration gradient was not so
- 78 good because it analysed only two points of
- 79 the height of micro-column.
- Thus, in this work we have changed the 80
- configuration of the installation instrument 81
- by applying the Digital Interferometry. The 82
- 83 new configuration enables the analysis of the
- concentration profile over the height of the 84
- micro-column. The system was validated 85

- using binary mixtures of Benchmark 86
- Fontainebleau (Platten et al. 2003). 87
- One of the benefits of this configuration is 88
- 89 that it measures the stationary separation in
- 90 without perturbing the mixture.
- 91 Therefore, it is going to be possible to analyse
- 92 the theory transitory
- 93 thermogravitational effect. In addition, it will
- 94 allow the convective stability analysis of
- 95 binary and ternary mixtures.
- 96 This article is organized as follows: in section
- 97 "Experimental setup", a brief description of
- 98 the micro-column and the design of new
- 99 configuration of the optical arrangement and
- image processing are explained. In section 100
- 101 "Results and discussion", the results of
- thermodiffusion coefficient 102 of binary
- 103 mixtures are shown. Finally, section
- "Conclusions" outlines the results. 104

105 2. Experimental setup

106 Thermogravitational micro-column

- 107 The thermogravitational micro-column used
- in this work is the same as in (Naumann et al.
- 2012) with a slight difference. Only the core 109
- part of the cell, shaping the gap of the micro-110
- 111 column, was replaced for the reason that the
- inlet and outlet were clogged up after 112
- multiple uses. Therefore, we improved the 113
- design to solve the problem. The new core
- 115 part was made with the same material Ketron
- PEEK and was manufactured in Denatek 116
- Engineering and 117 Manufacturing
- Technologies company with the greatest 118
- accuracy possible. After the manufacturing
- 120 process, the gap size was verified in
- 121 Mondragon University by MITUTOYO
- 122 **CRYSTA APEX** S-7106 precision
- 123 coordinate measuring machine see Fig.1.



125 Fig.1 Measurement of the gap with MITUTOYO 126 CRYSTA APEX S-7106 machine.

127 The measurements with this machine consists 128 on selecting several points near the gap 129 Fig. 2a on surface 1 and then changing Y axis,

selecting other points in surface 2, Fig.2b.

131 Finally, the distances between selected points

132 are calculated. The new gap thickness is

133 $Lx=0.51\pm0.025$ mm, the height of Lz=30 mm

and width of Ly=3 mm. 134

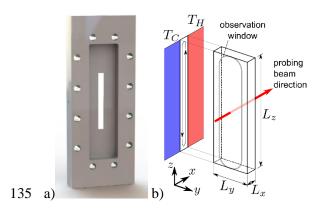


Fig.2 Core part of the micro-column, a) Shape of the gap of the micro-column, b) Configuration of the gap.

138 Design of the new configuration of optical 139 diagnostics

140 The new configuration of the installation is 141 based on Digital Interferometer (Mialdun and 142 Shevtsova 2011). The two main contributions

of this configuration are: On the one hand, all the height of the column is analysed as the 144

145 laser beam was expanded to cover all the

146 window of micro-column. On the other hand, 147 we introduced two lasers with different

148 wavelengths, a Diode-Pumped one with 149 $\lambda = 470 nm$

150 Fig.3 (1) and a He-Ne laser with $\lambda = 633nm$

wavelength (Spectra-Physics)

wavelength (Research Electro-Optics) to be 151

152 able to analyse also ternary mixtures in the

153 future; below in this section the all notations 154 refer to Fig.3. In order to work with both

155 lasers at the same time without mixing their 156 interference patterns, we have designed a special shutter system that is installed at the 157 exit aperture of each laser. This shutter system consists of a shaft moving up and 159 down (3) allowing or denying the pass of 160 161 laser beam. The movements of interrupter's 162 shaft and the acquisition of images are 163 synchronized by program implemented in 164 LabView (8).

After the shutting system, both laser beams 165 are passed from through neutral density 166 167 filters in order to adjust the intensityFig.3 (4). 168 Then, to expand the beams, we used two 169 spatial filter systems (Thorlab, KT310) with 170 an aspheric lens, a pinhole and a collimator in order to obtain a good quality beam (5). 171 Taking into account that the height of the 173 micro-column is 30 mm, the final beam 174 diameters were expanded to approximately 40 mm. Afterwards, both laser beams are 175 directed into a Mach-Zehnder interferometer 176 177 (6), where each beam is divided into two 178 equal beams. One passes through the microcolumn (7) (object beam) and the other one is 179 180 the reference beam. At the end of the 181 interferometer, divided beams are joined 182 creating an interference patterns that are acquired by CCD camera (QImaging 183 QIClick-CCD Camera) (9). 184

185 Digital interferometry is a trusted technique 186 that can be used to determine the 208

187 concentration of a mixture by analysing the 188 refractive index. The refractive index varies 189 because of a temperature and concentration 190 variations.

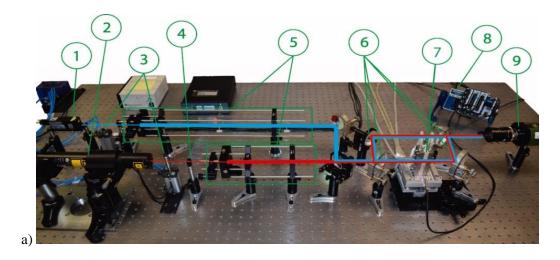
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$$\Delta n(y,z) = \left(\frac{\partial n}{\partial T}\right)_{T_o,c_o,\lambda} \Delta T(y,z) + \left(\frac{\partial n}{\partial c}\right)_{T_o,c_o,\lambda} \Delta c(y,z),$$

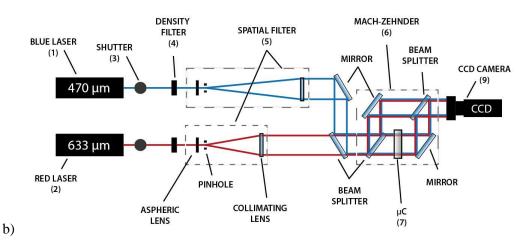
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Where, $(\partial n/\partial T)$ and $(\partial n/\partial c)$ are the contrast factors and $\Delta T(y,z)$ and $\Delta c(y,z)$ are the 195 temperature and concentration 196 spatial variations in vertical direction. In our system, 198 the temperature gradient is applied in the 199 same direction as the laser beam, so we can 200 omit the temperature variation $\Delta T(y, z)$ influence. Thus, the total variation of the 201 202 refractive index is due to the concentration variation (2). In turn, Δn is obtained from the 204 phase difference $\Delta \varphi$, which is measured by 205 the interferometry (3), where L_x is the 206 geometric path in liquid.

$$\Delta n(y,z) = \left(\frac{\partial n}{\partial c}\right)_{T_O,c_O,\lambda} \Delta c(y,z),\tag{2}$$

$$\Delta n(y,z) = \frac{\lambda}{2\pi L} \Delta \varphi(y,z)$$
 (3)





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211 Fig.3 Digital Interferometry applied to thermogravitational micro-column installation. a) Complete installation General view; 212 b) Scheme of the installation.

214 **Experimental** scenario **Image** and processing 215

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Both the interferometer configuration and image processing are based on Optical Digital Interferometry technique. Before starting the measurements, we stabilize the system at 25°C for 4 hours and acquire the images every 10 minutes in order to check the stability of the system. At the end of the measurement, one of the last acquired images in the stabilization step is taken as the reference image Fig.4. After applying the temperature gradient of $\Delta T = 8^{\circ} C$, the image acquisition rate is increased in order to see the evolution of phase variation in time. As the initial concentration change is bigger than near the stationary state, the acquisition of images is divided in three stages. For these binary mixtures, the image acquisition rate of first stage is 2 minutes during 36 minutes, in the second stage every 6 minutes during 72

minutes and finally every 12 minutes until the mixture reach the stationary state. 236

To extract the phase information from each 237 acquired image, we use the 2D Fourier 238 239 Transform technique described in literature (Mialdun and Shevtsova 2011). The Fig.4 240 outlines the image analysis steps. The phase information enables the determination of the refractive index of the sample. As a result, 243 knowing the concentration derivative of the 244 245 refractive index $(\partial n/\partial c)$ is possible to 246 determine the entire concentration profile 247 along the micro-column for each instant (for each acquired image). Once the mixture reach 248 249 the stationary stage, the slope of the 250 concentration along the height of the microcolumn $(\partial c/\partial z)$ is used in order to determine the thermodiffusion coefficient. 252

255 (bounded by white dashed lines in Fig.4).

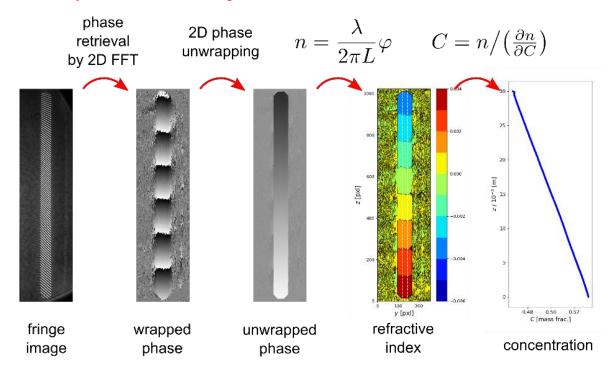


Fig.4 Steps for the phase information extraction of each acquired image.

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The concentration variation during the all experiment is shown in Fig.5. There it can be appreciate the stabilization process at 25°C for approximately 3-4 hours. Then, the temperature gradient is applied concentration in the sample start changing until mixture reach the stationary state. Negative concentration variation means that the reference component is enriched at the bottom part of the micro-column.

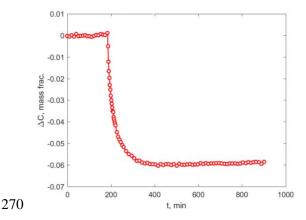


Fig.5 Separation of the concentration in time for measurement Time evolution of the concentration separation of THN-C12 binary mixture at 50% of mass fraction with $\Delta T = 8^{\circ} C$, monitored by and using 470nm wavelength.

3. Results and discussion

For the validation of the new analysis method, we have measured thermodiffusion coefficients of three binary mixtures at equal mass fraction of THN (purity, 98+%), IBB (purity, 99%) and C12 (purity, 99%). All measurements have been carried out at mean temperature of 25°C. The thermophysical properties as density, thermal expansion and dynamic viscosity were taken from (Alonso de Mezquia et al. 2015) and the contrast factor $(\partial n/\partial c)$ at 633 wavelength of three binary mixtures were was taken from (Gebhardt et al. 2013). To calculate the $(\partial n/\partial c)$ at 470 nm, Cauchy dispersion relation has been used as it is detailed in (Mialdun, A. and Shevtsova 2017). In Table 1, all the optical and thermophysical properties from taken literature are shown.

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298 Table 1. Optical and thermophysical properties of 299 THN-IBB-C12 binary mixtures at equal mass fraction 300 at 25°C. Density, thermal expansion and dynamic 301 viscosity are taken from (Alonso de Mezquia et al. 302 2015) and $(\partial n/\partial c)$ from (Gebhardt et al. 2013).

	THN-	THN-	IBB-
	C12	IBB	C12
ρ $\left(kg/m^3\right)$	841.248	904.514	792.355
$\alpha \times 10^{-3}$ (K^{-1})	0.895	0.888	0.961
$\mu \times 10^{-3}$ (Pas)	1.523	1.374	1.133
$(\partial n/\partial c)$ $(\lambda = 633nm)$	0.1155	0.0547	0.0625
$(\partial n/\partial c)$ $(\lambda = 470nm)$	0.1258	0.0577	0.0700

During the image processing, the concentration in the entire cross-section of the cell is determined in from each image. The Fig.6a shows the initial concentration profile when the micro-column is stabilized at 25°C and in Fig.6b when it reaches the stationary state with $\Delta T = 8^{\circ} C$.

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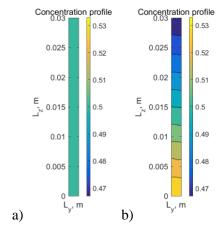
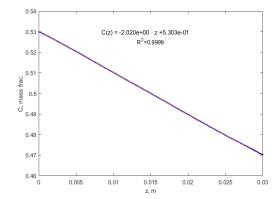


Fig.6 Concentration profiles inside the micro-column of filled with THN-C12 at 50 % mass fraction; a) when mixtures is stabilized at $25^{\circ} C$, b) when the mixtures reaches the stationary state after applying $\Delta T = 8^{\circ} C$.

316 Afterwards, the vertical concentration profile is represented in function of the height of the micro-column and is fitted polynomial of the first order obtaining $(\partial c/\partial z)$ as shown in Fig.7.



322 Fig.7 Concentration gradient at stationary state along 323 the height of the micro-column of THN-C12 at 50% mass fraction with $\Delta T = 8^{\circ} C$.

Finally, the thermodiffusion coefficient of binary mixtures is determined (4) (Larrañaga 326 et al. 2014), 327

$$D_T = -\frac{L_X^4}{504} \frac{g \alpha}{v C_0 (1 - C_0)} \frac{\partial c}{\partial z}$$
 (4)

where, L_{r} is the gap of the micro-column, g

is the gravity, α is the thermal expansion

330 coefficient, v is the kinematic viscosity and

331 C_0 is the initial concentration of the

332 reference component.

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The Table 2, Table 3 and Table 4 show the 333

thermodiffusion coefficients of THN-C12,

THN-IBB and IBB-C12 binary mixtures and 335

values with the respective 336 the mean

337 deviations.

338 The obtained results show a good agreement

339 Benchmark Fontainebleau

340 (Platten et al. 2003) so we have seen that the

new configuration provides reliable results 341

342 that makes us confident in reliability of the

343 new configuration.

344 the first time, with the 345 configuration, we have analysed all the 346 height of the column and we have seen the 347 entire concentration profile inside the 348 thermogravitational column.

Table 2. Thermodiffusion coefficients of THN-C12 binary mixtures at 50% mass fraction.

	633 nm		470 nm		Benchmark
THN-C12	$(\partial c/\partial z)$	$\begin{pmatrix} D_T \times 10^{-12} \\ \left(m^2 / sK\right) \end{pmatrix}$	$(\partial c/\partial z)$	$D_T \times 10^{-12} \left(m^2/sK\right)$	(Platten et al. 2003)
1	-2.124	5.53	-2.070	5.39	
2	-2.264	5.90	-2.177	5.66	
3	-2.304	5.99	-2.275	5.92	
4	-2.260	5.88	-2.180	5.68	
5	-2.299	5.99	-2.212	5.76	
Average	-2.250	5.86±0.33	-2.183	5.68±0.29	5.9±0.3

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Table 3. Thermodiffusion coefficients of THN-IBB binary mixtures at 50% mass fraction.

	63:	3 nm	470	470 nm	
THN-IBB	$(\partial c/\partial z)$	$\begin{pmatrix} D_T \times 10^{-12} \\ \left(m^2 / sK \right) \end{pmatrix}$	$(\partial c/\partial z)$	$\begin{pmatrix} D_T \times 10^{-12} \\ \left(m^2 / sK\right) \end{pmatrix}$	(Platten et al. 2003)
1	-1.062	3.27	-1.010	3.11	
2	-0.801	2.46	-0.794	2.44	
3	-0.844	2.60	-0.804	2.68	
4	-1.062	3.27	-0.983	3.03	
5	-0.937	3.03	-0.984	2.89	
6	-0.902	2.78	-0.877	2.70	
Average	-0.935	2.90±0.44	-0.909	2.81±0.37	2.8±0.1

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Table 4. Thermodiffusion coefficients of IBB-C12 binary mixtures at 50% mass fraction.

	633 nm		470	Benchmark	
IBB-C12	$(\partial c/\partial z)$	$\begin{pmatrix} D_T \times 10^{-12} \\ \left(m^2 / sK\right) \end{pmatrix}$	$(\partial c/\partial z)$	$\begin{pmatrix} D_T \times 10^{-12} \\ \left(m^2 / sK\right) \end{pmatrix}$	(Platten et al. 2003)
1	-1.079	3.82	-1.022	3.61	
2	-0.994	3.52	-0.987	3.49	
3	-1.209	4.28	-1.094	3.87	
4	-1.123	3.98	-1.074	3.80	
5	-1.146	4.06	-1.112	3.94	
6	-1.071	3.79	-0.988	3.49	
Average	-1.104	3.91±0.39	-1.046	3.70 ± 0.24	3.7±0.2

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355 **4. Conclusions**

356 In this work, we have changed the 357 configuration of the previously reported 358 optical analysis method applied 359 thermogravitational micro-column. The new 360 configuration of the interferometer and the image processing is based on Optical Digital 362 Interferometry analysis method. With the 363 new configuration, we are able to analyse the entire window of micro-column instead of analysing only two points. Thanks to this improvement, we are able to see the entire concentration profile inside the microcolumn during the measurements.

- 369 To validate the new system, we have 370 determined the thermodiffusion coefficients
- of three binary mixtures at equal mass
- fractions. Results have been compared with
- 373 Benchmark Fontainebleau

374 By tThe new analysis method in future it is

- 375 going to be possible can be readily extended
- 376 to analyse ternary mixtures. The analysis of the entire concentration profile will allow to 377
- study the thermogravitational effect in the 378
- 379 transitory state of binary and ternary
- 380 mixtures.

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Abstract

- In this work, we have applied Optical
- **Digital** Interferometry approach
- thermogravitational micro-column 10
- technique. 11
- By the new analysis, we examine the entire 12
- height of the micro-column and determine 13
- the complete concentration profile inside.
- The measurements were carried out by two 15
- lasers with different wavelength $\lambda = 633nm$ 16
- and $\lambda = 470nm$. The system was validated 17
- with binary subsystems of the THN-IBB-18
- C12 ternary mixture at equal mass fractions.
- 20 The results were compared with values of
- 21 Benchmark Fontainebleau and they showed
- an excellent agreement.
- Thermodiffusion, 23 **Keywords**: binary
- mixtures, Thermogravitational 24 micro-
- column, Optical Digital Interferometry.

1. Introduction 26

- Since over last decades, optical methods 27
- 28 have been widely used in the determination
- 29 of transport properties the
- thermodiffusion, molecular diffusion
- Soret coefficients of binary mixtures. For
- Deflection example, Optical Beam
- (Kolodner et al. 1988; Zhang et al. 1996),
- Optical Digital Interferometry (Mialdun and
- Shevtsova 2008) and Thermal Diffusion
- Forced Rayleigh Scattering (Wiegand et al.
- 2007; Wittko and Köhler 2003) have been
- used to analyse several binary mixtures. All
- these optical methods have demonstrated
- good sensitivity in measurements. 40
- 41 Now the challenge is focused on ternary
- 42 mixtures, so many of these techniques have
- been modified in order to analyse more

- complex systems. As a result, nowadays
- several instruments such as (Gebhardt et al.
- 2013) and (Mialdun et al. 2015) are able to
- determine the transport properties
- different ternary mixtures using optical 48
- analysis methods or by samples extraction 49
- (Larrañaga et al. 2015).
- Optical methods allow to work with small
- sample volume because the measurements
- are usually carried out in situ. In the case of
- biological substances, for instance, it is not
- 55 always easy or possible to obtain big
- The 56 samples. conventional
- thermogravitational 57 parallelepiped and
- cylindrical columns (Larrañaga et al. 2015b;
- Urteaga et al. 2012) need at least 30 ml of
- sample, so it is not viable to analyse
- biological samples using those techniques. 61
- For this reason, a new thermogravitational 62
- 63 micro-column was designed, constructed
- and validated in Mondragon University
- 65 (Naumann et al. 2012) in order to determine
- the thermodiffusion coefficient purely by 66
- optical method. The sample volume of this 67
- micro-column is less than 50 µl so it makes 68
- feasible the investigation of expensive 69
- substances, which cannot be obtained in 70
- large quantities. The optical approach 71
- 72 applied to the micro-column, made possible
- to analyse the continuous concentration 73
- 74 profile in binary mixtures between two
- points. Nevertheless, by this analysis method
- (Naumann et al. 2012), the accuracy of
- 77 determining the vertical concentration
- gradient was not so good because it analysed 78
- 79 only two points of the height of micro-
- column. 80
- Thus, in this work we have changed the 81
- 82 configuration of the instrument by applying
- Interferometry. 83 Digital The
- configuration enables the analysis of the 84
- concentration profile over the height of the 85

- 86 micro-column. The system was validated
- 87 using binary mixtures of Benchmark
- 88 Fontainebleau (Platten et al. 2003).
- 89 One of the benefits of this configuration is
- 90 that it measures the stationary separation in
- 91 situ without perturbing the mixture.
- 92 Therefore, it is going to be possible to
- 93 analyse the transitory theory of the
- 94 thermogravitational effect. In addition, it
- 95 will allow the convective stability analysis
- 96 of binary and ternary mixtures.
- 97 This article is organized as follows: in
- 98 section "Experimental setup", a brief
- 99 description of the micro-column and the
- 100 design of new configuration of the optical
- 101 arrangement and image processing ar
- 102 explained. In section "Results and
- 103 discussion", the results of thermodiffusion
- 104 coefficient of binary mixtures are shown.
- 105 Finally, section "Conclusions" outlines the
- 106 results.

107 **2. Experimental setup**

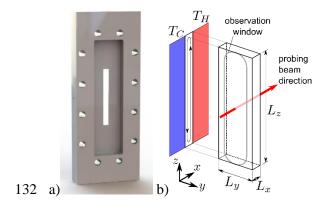
108 Thermogravitational micro-column

- 109 The thermogravitational micro-column used
- 110 in this work is the same as in (Naumann et
- 111 al. 2012) with a slight difference. Only the
- 112 core part of the cell, shaping the gap of the
- 113 micro-column, was replaced for the reason
- 114 that the inlet and outlet were clogged up
- 115 after multiple uses. Therefore, we improved
- 116 the design to solve the problem. The new
- 117 core part was made with the same material
- 118 Ketron PEEK and was manufactured in
- 119 Denatek Engineering and Manufacturing
- 120 Technologies company with the greatest
- 121 accuracy possible. After the manufacturing
- 122 process, the gap size was verified in
- 123 Mondragon University by MITUTOYO
- 124 CRYSTA APEX S-7106 precision
- 125 coordinate measuring machine see Fig.1.



127 Fig.1 Measurement of the gap with MITUTOYO 128 CRYSTA APEX S-7106 machine.

- 129 The new gap thickness is $Lx=0.51\pm0.025$
- 130 mm, the height of Lz=30 mm and width of
- 131 Ly=3 mm.



133 Fig.2 Core part of the micro-column, a) Shape of the 134 gap of the micro-column, b) Configuration of the gap.

135 **Design of the new configuration of optical** 136 **diagnostics**

The new configuration of the installation is 137 based on Digital Interferometer (Mialdun 138 and Shevtsova 2011). The two main 139 contributions of this configuration are: On 141 the one hand, all the height of the column is 142 analysed as the laser beam was expanded to 143 cover all the window of micro-column. On the other hand, we introduced two lasers 144 with different wavelengths, a Diode-Pumped one with $\lambda = 470 nm$ wavelength (Spectra-Physics) Fig.3 (1) and a He-Ne laser with 148 $\lambda = 633nm$ wavelength (Research Electro-149 Optics) to be able to analyse also ternary 150 mixtures in the future; below in this section 151 the all notations refer to Fig.3. In order to 152 work with both lasers at the same time without mixing their interference patterns, 153 154 we have designed a special shutter system that is installed at the exit aperture of each 155 laser. This shutter system consists of a shaft 156 moving up and down (3) allowing or

denying the pass of laser beam. The 158

159 movements of interrupter's shaft and the

160 acquisition of images are synchronized by

program implemented in LabView (8). 161

162 After the shutting system, both laser beams

are passed through neutral density filters in

order to adjust the intensityFig.3 (4). Then,

to expand the beams, we used two spatial 165

filter systems (Thorlab, KT310) with an 166

167 aspheric lens, a pinhole and a collimator in

order to obtain a good quality beam (5). 168

Taking into account that the height of the

170 micro-column is 30 mm, the final beam

171 diameters were expanded to approximately

40 mm. Afterwards, both beams are directed 172

into a Mach-Zehnder interferometer (6), 173

where each beam is divided into two equal

175 beams. One passes through the micro-

column (7) (object beam) and the other one

177 is the reference beam. At the end of the

interferometer, divided beams are joined

178 creating an interference patterns that are

179

180 acquired by CCD camera (QImaging

QIClick-CCD Camera) (9). 181

Digital interferometry is a trusted technique

that can be used to determine 183

184 concentration of a mixture by analysing the

refractive index. The refractive index varies 185

186 because of a temperature and concentration

187 variations,

188
$$\Delta n(y,z) = \left(\frac{\partial n}{\partial T}\right)_{T,C,A} \Delta T(y,z) + \left(\frac{\partial n}{\partial c}\right)_{T,C,A} \Delta c(y,z),$$

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Where, $(\partial n/\partial T)$ and $(\partial n/\partial c)$ are the contrast 191

factors and $\Delta T(y,z)$ and $\Delta c(y,z)$ are the

193 spatial temperature and concentration

194 variations. In our system, the temperature

195 gradient is applied in the same direction as

the laser beam, so we can omit the 196

temperature variation $\Delta T(y, z)$ influence. 197 Thus, the total variation of the refractive

199 index is due to the concentration variation

(2). In turn, Δn is obtained from the phase 200

201 difference $\Delta \varphi$, which is measured by the

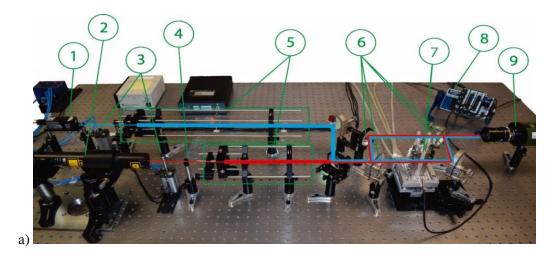
202 interferometry (3), where Lx is the

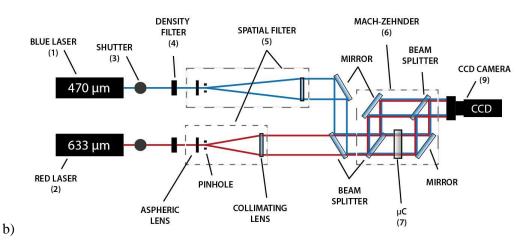
203 geometric path in liquid.

$$\Delta n(y,z) = \left(\frac{\partial n}{\partial c}\right)_{T_{\alpha},c_{\alpha},\lambda} \Delta c(y,z), \tag{2}$$

$$\Delta n(y,z) = \frac{\lambda}{2\pi L} \Delta \varphi(y,z)$$
 (3)

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208 Fig.3 Digital Interferometry applied to thermogravitational micro-column installation. a) General view; b) Scheme of the 209 installation.

211 **Experimental** scenario **Image** and processing 212

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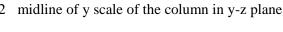
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Both the interferometer configuration and image processing are based on Optical Digital Interferometry technique. Before starting the measurements, we stabilize the system at 25°C for 4 hours and acquire the images every 10 minutes in order to check the stability of the system. At the end of the 219 220 measurement, one of the last acquired images in the stabilization step is taken as the reference image. After applying the 222 temperature gradient of $\Delta T = 8^{\circ} C$, the image 223 acquisition rate is increased in order to see the evolution of phase variation in time. As the initial concentration change is bigger than near the stationary state, the acquisition of images is divided in three stages. For these binary mixtures, the image acquisition rate of first stage is 2 minutes during 36 minutes, in the second stage every 6 minutes

during 72 minutes and finally every 12 minutes until the mixture reach 233 234 stationary state.

235 To extract the phase information from each acquired image, we use the 2D Fourier 236 Transform technique described in literature 237 238 (Mialdun and Shevtsova 2011). The Fig.4 239 outlines the image analysis steps. The phase information enables the determination of the 240 241 refractive index of the sample. As a result, knowing the concentration derivative of the 242 refractive index $(\partial n/\partial c)$ is possible to 243 determine the entire concentration profile along the micro-column for each instant (for each acquired image). Once the mixture reach the stationary stage, the slope of the 247 concentration along the height of the micro-248 $(\partial c/\partial z)$ is used in order to 249 column determine the thermodiffusion coefficient. 250



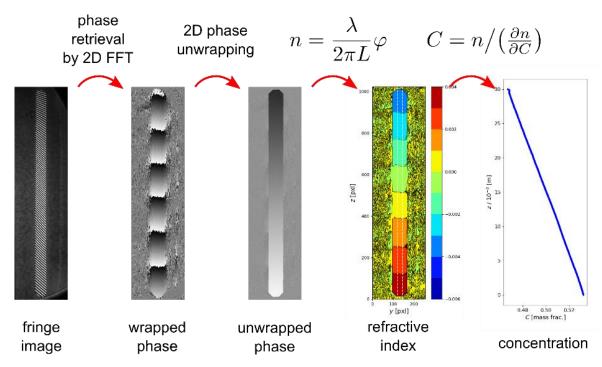


Fig.4 Steps for the phase information extraction of each acquired image.

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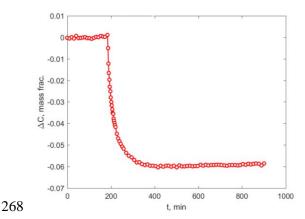
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The concentration variation during the all experiment is shown in Fig.5. There it can be appreciate the stabilization process at 25°C for approximately 3-4 hours. Then, the temperature gradient is applied so concentration in the sample start changing until mixture reach the stationary state. Negative concentration variation means that the reference component is enriched at the bottom part of the micro-column.



269 Fig.5 Time evolution of the concentration separation 270 of THN-C12 binary mixture at 50% of mass fraction 271 with $\Delta T = 8^{\circ} C$, monitored by 470nm wavelength.

72 3. Results and discussion

273 For the validation of the new analysis 274 method, have we measured the 275 thermodiffusion coefficients of three binary 276 mixtures at equal mass fraction of THN 277 (purity, 98+%), IBB (purity, 99%) and C12 278 (purity, 99%). All measurements have been 279 carried out at mean temperature of 25°C. 280 The thermophysical properties as density, 281 thermal expansion and dynamic viscosity 282 were taken from (Alonso de Mezquia et al. 283 2015) and the contrast factor $(\partial n/\partial c)$ at 633 284 nm wavelength of three binary mixtures was taken from (Gebhardt et al. 2013). To 285 calculate the $(\partial n/\partial c)$ at 470 nm, Cauchy 286 dispersion relation has been used as it is 288 detailed in (Mialdun, A. and Shevtsova 2017). In Table 1, all the optical and 289 290 thermophysical taken properties from 291 literature are shown.

Table 1. Optical and thermophysical properties of
 THN-IBB-C12 binary mixtures at equal mass fraction
 at 25°C. Density, thermal expansion and dynamic

	THN-	THN-	IBB-
	C12	IBB	C12
ρ $\left(kg/m^3\right)$	841.248	904.514	792.355
$\alpha \times 10^{-3}$ (K^{-1})	0.895	0.888	0.961
$\mu \times 10^{-3}$ (Pas)	1.523	1.374	1.133
$(\partial n/\partial c)$ $(\lambda = 633nm)$	0.1155	0.0547	0.0625
$(\partial n/\partial c)$ $(\lambda = 470nm)$	0.1258	0.0577	0.0700

During the image processing, the concentration in the entire cross-section of the cell is determined from each image. The Fig.6a shows the initial concentration profile when the micro-column is stabilized at 25°C and in Fig.6b when it reaches the

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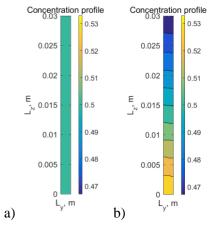
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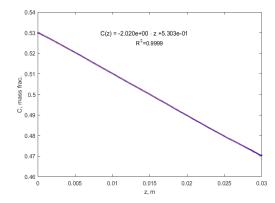
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stationary state with $\Delta T = 8^{\circ}C$.

Fig.6 Concentration profiles inside the micro-column filled with THN-C12 at 50 % mass fraction; a) when mixtures is stabilized at 25° C, b) when the mixture reaches the stationary state after applying $\Delta T = 8^{\circ} C$.

310 Afterwards, the vertical concentration 311 profile is represented in function of the 312 height of the micro-column and is fitted with 313 the polynomial of the first order obtaining 314 $(\partial c/\partial z)$ as shown in Fig.7.



316 Fig.7 Concentration gradient at stationary state along 317 the height of the micro-column of THN-C12 at 50% 318 mass fraction with $\Delta T = 8^{\circ} C$.

319 Finally, the thermodiffusion coefficient of 320 binary mixtures is determined (4) (Larrañaga 321 et al. 2014),

$$D_T = -\frac{L_X^4}{504} \frac{g \alpha}{v C_0 (1 - C_0)} \frac{\partial c}{\partial z}$$
 (4)

322 where, L_{x} is the gap of the micro-column,

323 g is the gravity, α is the thermal expansion

324 coefficient, v is the kinematic viscosity and

325 C_0 is the initial concentration of the

326 reference component.

327 The Table 2, Table 3 and Table 4 show the

328 thermodiffusion coefficients of THN-C12,

329 THN-IBB and IBB-C12 binary mixtures and

330 the mean values with the respective

331 deviations.

315

332 The obtained results show a good agreement

333 with Benchmark Fontainebleau values

334 (Platten et al. 2003) that makes us confident

335 in reliability of the new configuration.

336 For the first time, with the new

337 configuration, we have analysed all the

338 height of the column and we have seen the

339 entire concentration profile inside the

340 thermogravitational column.

Table 2. Thermodiffusion coefficients of THN-C12 binary mixtures at 50% mass fraction.

1	63			0 nm	Benchmark
THN-C12	$(\partial c/\partial z)$	$\begin{pmatrix} D_T \times 10^{-12} \\ \left(m^2 / sK \right) \end{pmatrix}$	$(\partial c/\partial z)$	$\binom{D_T \times 10^{-12}}{\binom{m^2}{sK}}$	(Platten et al. 2003)
1	-2.124	5.53	-2.070	5.39	
2	-2.264	5.90	-2.177	5.66	
3	-2.304	5.99	-2.275	5.92	
4	-2.260	5.88	-2.180	5.68	
5	-2.299	5.99	-2.212	5.76	
Average	-2.250	5.86±0.33	-2.183	5.68±0.29	5.9±0.3

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Table 3. Thermodiffusion coefficients of THN-IBB binary mixtures at 50% mass fraction.

	63	3 nm	470 nm		Benchmark
THN-IBB	$(\partial c/\partial z)$	$\frac{D_T \times 10^{-12}}{\left(m^2/sK\right)}$	$(\partial c/\partial z)$	$\begin{pmatrix} D_T \times 10^{-12} \\ \left(m^2 / sK\right) \end{pmatrix}$	(Platten et al. 2003)
1	-1.062	3.27	-1.010	3.11	
2	-0.801	2.46	-0.794	2.44	
3	-0.844	2.60	-0.804	2.68	
4	-1.062	3.27	-0.983	3.03	
5	-0.937	3.03	-0.984	2.89	
6	-0.902	2.78	-0.877	2.70	
Average	-0.935	2.90±0.44	-0.909	2.81±0.37	2.8±0.1

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Table 4. Thermodiffusion coefficients of IBB-C12 binary mixtures at 50% mass fraction.

IBB-C12	$(\partial c/\partial z)$	$ D_T \times 10^{-12} $ $ \left(\frac{m^2}{sK} \right) $	$(\partial c/\partial z)$	$ \begin{array}{c} D_T \times 10^{-12} \\ \left(m^2/sK\right) \end{array} $	Benchmark (Platten et al. 2003)
1	-1.079	3.82	-1.022	3.61	
2	-0.994	3.52	-0.987	3.49	
3	-1.209	4.28	-1.094	3.87	
4	-1.123	3.98	-1.074	3.80	
5	-1.146	4.06	-1.112	3.94	
6	-1.071	3.79	-0.988	3.49	
Average	-1.104	3.91±0.39	-1.046	3.70±0.24	3.7±0.2

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360

4. Conclusions

348 In this work, we have changed the 349 configuration of the previously reported 350 optical analysis method applied 351 thermogravitational micro-column. The new 352 configuration of the interferometer and the 353 image processing is based on Optical Digital 354 Interferometry analysis method. With the 355 new configuration, we are able to analyse 356 the entire window of micro-column instead of analysing only two points. Thanks to this improvement, we are able to see the entire 358 concentration profile inside the micro-359 column during the measurements.

- 361 To validate the new system, we have 362 determined the thermodiffusion coefficients
- 363 of three binary mixtures at equal mass
- 364 fractions. Results have been compared with
- 365 Benchmark Fontainebleau

366 The new analysis method can be readily

- 367 extended to analyse ternary mixtures. The
- 368 analysis of the entire concentration profile
- will allow to study the thermogravitational
- 370 effect in the transitory state of binary and
- ternary mixtures. 371

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