

Context-Informed Conditional Anomaly Detection Approach for Wave Power Plants: The Case of Air Turbines

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Abstract

The reliability and energy production of wave power plants (WPPs) depend on sea-state conditions, operation efficiency and degradation of its constituent assets. Air turbines are key assets for the efficient and reliable operation of WPPs and ensuring their correct operation leads to enhance the efficiency of WPPs. However, the lack of run-to-failure data and scarce fault records hampers the development of predictive condition monitoring solutions. In this context, focusing on unsupervised health monitoring methods, this paper presents an air turbine conditional anomaly detection (CAD) approach with a practical case study tested and validated on the Mutriku wave power plant. In contrast to anomaly detection models, which model the health-state without taking into account the influence of the operating context, the proposed CAD approach learns the expected air turbine operation conditioned on specific sea-states information modelled through wave energy flux concepts. This is achieved through an ensemble of Gaussian Mixture models and the expectation-maximization algorithm. Results show that, the integration of sea-states in the anomaly detection learning process improves the discrimination capability of the CAD model compared with the anomaly detection model without sea-state information, reducing false positive events and improving the accuracy of the CAD model.

Keywords: Marine Renewable Energy Monitoring, Anomaly Detection, Prognostics and Health Management, Turbine, Power Curve and Monitoring.

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1. Introduction

The ocean environment hampers the commercial viability of Marine Renewable Energy (MRE) technologies owing to the complexity to conceive balanced designs with the capacity to maximise energy harnessing and survivability, without excessive over-engineering. The harsh ocean environment accelerates the degradation of the different components of MRE devices and maintenance operations for offshore plants are significantly more complex and costly due to the limited accessibility, and the highly specialised vessel and crew requirements. Therefore, condition monitoring of MRE technologies is crucial because apart from the high maintenance cost, no energy is generated during longer downtimes.

In fact, production losses due to unavailability can result in downtime losses of up to 24 k€/MW (12 M€/year for a 500 MW offshore wind farm) [Rinaldi et al. \(2021b\)](#). As a consequence, operation and maintenance (O&M) costs associated with an offshore farm are estimated to be approximately 30% of the total income (for a 20-year lifetime), as opposed to 10-15% O&M costs associated with onshore farms [Sorensen & Sorensen \(2012\)](#).

However, due to the vast energy resource available in the ocean and more appealing characteristics of this resource, *e.g.* predictability and consistency, MRE systems are foreseen to be a key resource in the short- and long-term roadmaps towards a carbon-neutral energy system [European Commission Communication \(2020, 2019\)](#). The annual energy generation potential for offshore wind and wave is estimated in 420,000TWh [IEA \(2019\)](#) and 29,500TWh [Mørk et al. \(2010\)](#), respectively, representing together 19.5 times the current global electricity demand approximately.

Therefore, in order to make MRE technologies commercially viable, the development of intelligent and efficient O&M strategies is vital. These strategies should include, at least, the following four aspects:

1. Prediction of resource characteristics to assess plant accessibility.
2. Evaluation of MRE plant availability updated with condition-monitoring models.
3. Prediction of energy generation capabilities of the MRE plant.
4. Assessment of downtime and O&M costs.

The literature shows studies on some of these aspects, especially focusing on the more mature offshore wind industry. The accessibility of offshore wind farms is covered by [Guanche et al. \(2016\)](#), where a methodology to assess the accessibility to a floating wind turbine is evaluated concluding that the accessibility-limiting wave height threshold is highly dependent on wave direction and peak period. More recently, [Gilbert et al. \(2021\)](#) suggests a novel probabilistic method focused on forecasting safety-critical accessibility conditions.

Similarly, several condition monitoring approaches for offshore wind turbines components are present in the literature, such as turbine blades [Martinez-Luengo et al. \(2016\)](#), power transmission systems [Feng et al. \(2013\)](#), electric generators [Vedreño-Santos et al. \(2014\)](#) and power electronic components [Jlassi et al. \(2015\)](#). In addition to the component-level solutions, system-level methods have been also developed analysing component interactions

40 and their impact on the system Santos et al. (2015). Overall, Mérigaud & Ringwood (2016)
41 provides a comprehensive review of different methodologies and applications.

42 The prediction of energy generation capabilities have also been widely covered in the
43 literature for different MRE technologies. Based on the wave climate of a specific location,
44 the energy generation capabilities have been predicted using the capacity factor of the de-
45 vice/plant for longer periods Yue et al. (2019), power curves Gupta & Nem (2016) methods,
46 or more sophisticated dynamic models that are usually suggested for floating offshore wind
47 turbines (FOWTs) Cottura et al. (2021).

48 The economical evaluation of downtime and O&M services is also widely covered for
49 wind turbines, including offshore wind turbines. A common metric of the economic aspects
50 is the Levelised Cost of Energy (LCoE), which has been analysed in the literature for fixed
51 offshore wind turbines Ioannou et al. (2018) and FOWTs Martinez & Iglesias (2022). In
52 fact, Rinaldi et al. (2021a) incorporated the O&M models into the techno-economic analysis
53 of FOWTs.

54 While some of the methodologies suggested for offshore wind have a direct application on
55 the wave energy sector, *e.g.* accessibility models and part of the cost analysis, differences in
56 the energy harnessing process makes necessary to develop novel methods. Energy generation
57 prediction models, for example, are widely covered for different devices, with a wide variety
58 of modelling techniques and complexities Penalba & Ringwood (2016). However, mainly due
59 to the immaturity of the wave energy sector, prognostics and health management (PHM)
60 solutions are scarce. In fact, operational data covering relatively long periods of time is
61 often used for the different PHM studies, which does not exist in the case of wave energy.
62 This data can also be replaced with run-to-failure data generated in laboratory environment
63 through accelerated ageing tests, but these datasets are very limited to the best of authors'
64 knowledge.

65 One of the very few exceptions worldwide is the Mutriku Wave Power Plant (WPP),
66 further described later in Section 4. The Mutriku WPP is a wave energy conversion plant
67 based on the oscillating water column (OWC) technology commissioned by the Basque
68 Energy Agency in 2011 Torre-Enciso et al. (2009). It is one of the pioneer grid-connected
69 WPPs worldwide. It has been operating for the last 10 years, reporting different degradation
70 and failure events for different components. Due to the easily accessible location of the WPP,
71 maintenance operations are not the most critical aspect. However, the generated data is
72 highly valuable to develop PHM applications that will be vital for the reliable operation of
73 future WPPs located far from shore.

74 The authors intentionally focus on the anomaly detection problem, motivated by the lack
75 of run-to-failure data and scarce fault records. The operation of WPPs is highly variable, as
76 is the ocean resource, and accordingly, the anomaly detection problem becomes a challenging
77 task. Usually, anomalies are identified by comparing the plant operation against pre-defined
78 normal behaviour. When a variable differs from what is expected under normal operating
79 conditions, it may flag an anomaly. However, when the normal behaviour is highly-variable,
80 the definition of conditions that represents the normal behaviour is a challenging task.
81 Therefore, an accurate anomaly detection technique for WPPs requires information about
82 the operation context to reduce false positives.

In fact, to the best of authors' knowledge, such a context-informed anomaly detection framework for WPPs has never been suggested in the literature. Hence, this paper presents a novel conditional anomaly detection approach focused on air turbines operated in OWC devices, where the context information is represented by sea-state conditions. The approach has been tested in the Mutriku WPP and results show that the integration of environmental sea-state information along with WPP parameters in the anomaly detection learning process, improves the discrimination capability of the CAD model compared with the anomaly detection model without sea-state information, reducing false positive events and improving the accuracy of the conditional anomaly detection model.

The remainder of this paper is organised as follows. Section 2 presents the integrated PHM framework for WPPs and reviews more specific state-of-the-art for anomaly detection problems. Section 3 presents the conditional anomaly detection model developed within the PHM framework. Section 4 presents the Mutriku WPP case study and Section 5 shows results by applying the developed approach to the case study. Section 6 discusses the proposed approach and Section 7 draws conclusions.

2. PHM framework for Wave Power Plants

Figure 1 shows the block diagram of the integrated PHM framework for a generic WPP. The framework combines expert knowledge of plant engineers with collected data to detect anomalies, diagnose failure causes, and predict the remaining useful life (RUL) of plant components [Aizpurua & Catterson \(2015\)](#).

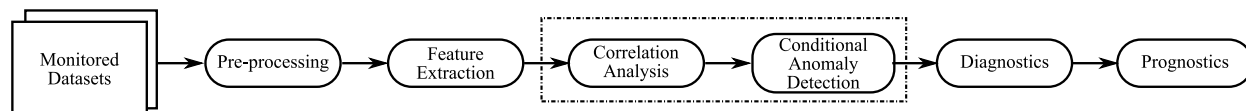


Figure 1: PHM framework for a generic WPP, highlighting the focus of this work.

Monitored variables of the WPP are firstly processed to discard missing and invalid values and filter noisy signals. Then pre-processed datasets are used to extract features that represent plant health information in different statistical, temporal and frequency domains. After the feature extraction step, the correlation analysis informs about dependencies between variables. These dependencies can be post-processed to develop different applications, such as the identification of deviations from normal operation conditions through changes in dependencies.

Anomaly detection models focus on the identification of deviations from expected normal operation conditions. They can be useful to define alarm systems or trigger further predictive analysis activities and react to the observed condition. Diagnostics models focus on the identification of the actual health state [Vachtsevanos et al. \(2006\)](#). This classification can be based on predefined groups of health states or it can be centred on the estimation of the actual health state through *e.g.* filtering strategies [Aizpurua et al. \(2020\)](#). Prognostics models focus on the prediction of future degradation trajectories and RUL estimation based on likely life-stressors and operational profiles [Aizpurua et al. \(2019\)](#). This research

118 focuses on the development of an adequate anomaly detection approach and development of
119 diagnostics and prognostics models within the PHM framework are left for future work (cf.
120 Section 7).

121 There exist limited monitoring solutions for marine energy applications, such as tidal
122 turbine degradation modelling [Galloway et al. \(2017\)](#), or wave energy converter health mon-
123 itoring through underwater acoustic emission [Walsh et al. \(2017\)](#). The development of
124 monitoring solutions for tidal turbines and wave energy applications based on power curve
125 modelling is a challenging approach, because it is necessary to model the sea-state infor-
126 mation and evaluate its influence on the generated power [Mérigaud & Ringwood \(2016\)](#).
127 Technological solutions for wind energy have been developed for many years now and, ac-
128 cordingly, most of the proposed turbine condition monitoring solutions focus on wind tur-
129 bines [de Novaes Pires Leite et al. \(2018\)](#). Technological similarities between air-turbines
130 implemented in OWC devices and wind turbines suggest that methodologies applied on
131 wind turbines may be applicable to air-turbines.

132 Wind turbine anomaly detection approaches can be classified into data-driven and model-
133 based approaches [Hameed et al. \(2009\)](#); [Kusiak et al. \(2013\)](#). Model-based methods develop
134 physics-based operational models and data-driven methods define the expected operation
135 through operational data measured via supervisory control and data acquisition (SCADA)
136 systems. Anomaly detection models for wind turbines have often been addressed in the
137 literature through probabilistic power curve models using statistical learning models, such
138 as copulas [Gill et al. \(2012\)](#) and Gaussian processes [Pandit & Infield \(2018\)](#).

139 In other engineering contexts, different unsupervised anomaly detection approaches have
140 been proposed. [Vanem & Brandsæter \(2021\)](#) evaluate different unsupervised anomaly detec-
141 tion methods tested on marine diesel engine data, including Self-Organising Maps (SOM),
142 k Nearest-Neighbor (kNN), density-based clustering (DBscan), Gaussian Mixture Models
143 (GMM) and one-class Support Vector Machines (SVM). They provide an insightful dis-
144 cussion about the hyper-parameter selection, relevance of training data and the effect of
145 dimensionality reduction. [Coraddu et al. \(2019\)](#) develop two anomaly detection models
146 using kNN and SVM models to monitor hull and propeller performance. These unsuper-
147 vised anomaly detection models, evaluate the available dataset to explore anomalies without
148 ground truth information. In [Vanem & Brandsæter \(2021\)](#) different models are tested and
149 it is possible to validate results by checking the consistency across models. In [Coraddu et al.](#)
150 [\(2019\)](#) labels are used to evaluate the performance of the anomaly detection models.

151 In a similar direction, [Baraldi et al. \(2015\)](#) presented an application of the Auto-Associative
152 Kernel Regression (AAKR) approach [Hines & Garvey \(2006\)](#), which focuses on fitting normal
153 data to a AAKR model, subsequent signal reconstruction and comparison with monitored
154 parameters. The performance of the approach is dependent on the learned signal prop-
155 erties and it has been enhanced in [Brandsæter et al. \(2019\)](#) for large datasets including
156 memory vectors modelled as clusters. So as to enhance the learning abilities of anomaly
157 detection models, autoencoder (AE) architectures were proposed building representations
158 of the original signal encoded in deep Artificial Neural Network layers, and then evaluate
159 reconstructions of monitored signals with the designed AE model, which can integrate signal
160 properties in the different neurons and layers of the AE model [Wu et al. \(2020\)](#). AAKR

161 and AE models, perform adequately in controlled environments and they have shown an
162 excellent ability to learn independent signal properties over time. However, they lack of
163 contextual information.

164 Anomaly detection without contextual information is a challenging task, which can cre-
165 ate spurious jumps in the data and penalize the performance of the anomaly detection
166 model [Vanem & Brandsæter \(2021\)](#). In this direction, so as to cover the range of operation
167 and reduce false positives, ensemble strategies have been proposed by combining multiple
168 anomaly detection models, such as the ensemble of hidden Markov models combined through
169 kappa measurements to reach diversity and detect multiple anomalies [Islam et al. \(2018\)](#).
170 Recently, transfer learning concepts have been also implemented to complement operational
171 data with different operation conditions through adversarial deep-learning concepts [Michau
172 & Fink \(2021\)](#).

173 It can be observed that existing anomaly detection models perform appropriately under
174 stable operation conditions, but show a poor performance without contextual information.
175 This can be partially handled with an ensemble of anomaly detection models, but it is nec-
176 essary to design multiple and diverse models that can capture characteristics of different
177 operation conditions. The operation and degradation of WPP is strongly influenced by
178 metocean conditions [Mérigaud & Ringwood \(2016\)](#), and in such cases, it is necessary to
179 incorporate sea-state information in the modelling process. One possibility to achieve this
180 objective is the adoption of conditional anomaly detection (CAD) modelling concepts [Song
181 et al. \(2007\)](#), where the main goal is to learn and model the normal operation condition
182 of the system as a function of the operation context. [Catterson et al. \(2010\)](#) presented a
183 conditional anomaly detection model for transformer monitoring taking into account envi-
184 ronmental parameters such as meteorological conditions and applied electrical load, along
185 with transformer condition data such as oil temperature and dissolved gasses.

186 However, to the best of authors' knowledge, contextual anomaly detection concepts have
187 not been developed for wave power plants and this is the original contribution of this paper.
188 The proposed approach makes use of unsupervised machine learning methods so as to model
189 air turbine operation states, which are statistically correlated with contextual sea-state
190 information to learn likely normal operation states along with associated sea-state conditions.
191 The approach is tested and validated with real data collected in the Mutriku WPP, including
192 fault events that are used to validate the proposed model.

193 **3. Air-Turbine Conditional Anomaly Detection Approach**

194 The main focus of this paper is on the development of a CAD model for air turbines
195 operated in WPPs. The implementation of this approach will permit the prompt detection
196 of anomalies while avoiding false positives and unplanned maintenance actions.

197 The expected operation of an air turbine can be modelled using the characteristic power
198 curve, which relates the rotation speed with the produced power. Figure 2 shows the power
199 curve of the turbine T10 of the Mutriku WPP using the monitored SCADA data corre-
200 sponding to 10/09/2019-10/12/2019. It can be observed that the saturation point is located
201 near 3200 rpm with an approximated maximum produced power of 22 kW. Negative power

202 values indicate that the WPP absorbs energy from the grid to prevent the turbine from
 203 stopping.

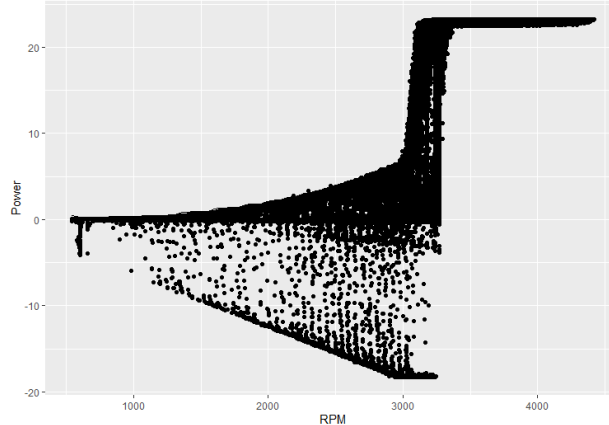


Figure 2: Mutriku WPP power curve.

204 Deviations from the characteristic power curve may indicate early warnings or abnormal
 205 turbine operation states [Gill et al. \(2012\)](#). However, the operation of air turbines is
 206 surrounded by different sources of uncertainty, such as stochastic sea-state and atmospheric
 207 conditions, and accordingly, it is necessary to capture uncertainty modelling criteria along
 208 with the power curve.

209 In the context of anomaly detection models, it is crucial to reduce false positives and
 210 maximize accuracy. Different operation conditions may result in different performance indi-
 211 cators, and therefore, it is very important to learn the normal behaviour of the turbine with
 212 respect to its operation context.

213 Accordingly, this paper defines a framework to jointly model expected turbine perfor-
 214 mance conditions along with the corresponding expected sea-state. Figure 3 shows the
 215 developed conditional anomaly detection model for the air turbine, where turbine operation
 216 data is combined with environmental conditions and the operation of the turbine is evaluated
 217 conditioned to the environmental information.

218 The environmental model will be determined through the combination of significant wave
 219 height H_s and the peak period T_p , which are common statistical parameters to characterize
 220 a sea-state [Ardhuin et al. \(2019\)](#). Subsequently, probabilistic multivariate models will be
 221 developed for the turbines to characterize the corresponding probabilistic power curve of
 222 the turbine. Finally, their probabilistic correlations will be defined so as to estimate the
 223 probability of a turbine being healthy, given the operational information.

224 3.1. Environmental sea-state model

225 The environmental model will be defined through the wave energy flux (WEF), which
 226 models the energetic sea-state, and it is defined as follows:

$$WEF = 0.49 H_s^2 T_e, \quad (1)$$

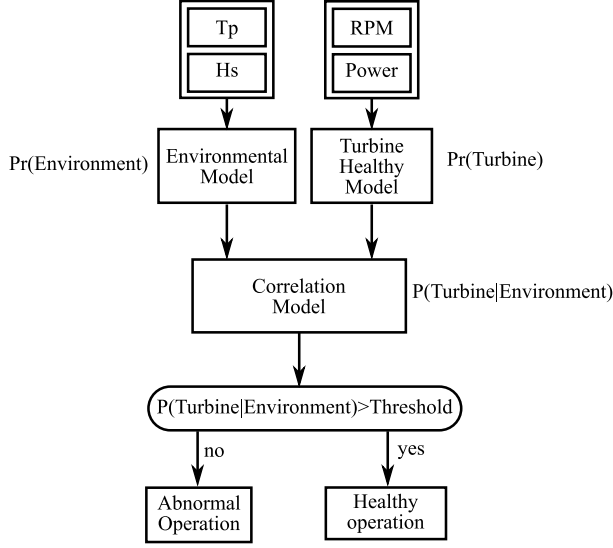


Figure 3: CAD framework for air turbines.

227 where T_e is the energetic period defined as follows:

$$T_e = \alpha T_p \quad (2)$$

228 where $\alpha = 0.9$ is considered as suggested in Tucker & Pitt (2001).

229 It is expected that higher energetic sea-states, that are characterized with high WEF
 230 values, will operate with a different power curve compared with low energetic sea-states.
 231 Accordingly, the expected operation conditions, including the rotational speed and generated
 232 power, will be different depending on the sea-state.

233 In this paper, different sea-states have been organized into different levels according to
 234 their energy flux values (see Section 4). The classification criteria is solely based on expert-
 235 knowledge and the use of data-driven clustering strategies is left for future work.

236 3.2. Air Turbine model

237 The power curve of the air turbine model will be developed using multivariate probabilis-
 238 tic distributions through Gaussian Mixture Models (GMM) Song et al. (2007). GMMs can
 239 model multivariate distributions and they enable capturing uncertainties through mixture
 240 of Gaussian distributions.

241 For each power curve sample, comprised of the pair $x_i = \{r_i, e_i\}$, where r denotes the
 242 rotational speed of the generator (in rpm units), and e denotes the generated energy (in kW
 243 units), the PDF of the GMM, $f_{GMM}(x_i)$, is defined through a set of Gaussian distributions
 244 $k \in \{1, \dots, K\}$ mixed in different proportions:

$$f_{GMM}(x_i|\Theta) = \sum_{k=1}^K \alpha_k P(x_i|\theta_k) \quad (3)$$

245 where $\{\alpha_1, \dots, \alpha_K\}$ are the mixing probabilities, each θ_k is the set of parameters defining the
 246 k -th component, and Θ is the complete set of parameters needed to specify the mixture,
 247 $\Theta \equiv \{\theta_1, \dots, \theta_K, \alpha_1, \dots, \alpha_K\}$.

248 In the univariate case, the likelihood of new measurements x_i given the GMM parameters,
 249 $P(x_i|\theta_k)$, is defined as follows:

$$P(x_i|\theta_k) = \frac{1}{\sigma_k(\sqrt{2\pi})} \exp\left(-\frac{1}{2} \frac{(x_i - \mu_k)^2}{\sigma_k^2}\right) \quad (4)$$

250 where σ_k^2 is the variance and $\theta_k = \{\mu_k, \sigma_k\}$.

251 Eqs. (3) and (4) define the GMM model for the univariate case. They are extended for
 252 the multi-dimensional case by defining the likelihood function as follows:

$$P(x_i|\theta_k) = \frac{1}{(2\pi^d \det|\Sigma_k|)^{\frac{1}{2}}} \exp\left(-\frac{1}{2}(x_i - \mu_k)^T \Sigma_k^{-1} (x_i - \mu_k)\right) \quad (5)$$

253 where d is the dimension of the data, μ_k is the mean vector, Σ_k is the covariance matrix,
 254 and $\theta_k = \{\mu_k, \Sigma_k\}$.

255 Given a set of n data samples, $\mathbf{X} = \{x_1, \dots, x_n\}$, the log-likelihood corresponding to a
 256 k -th component mixture is:

$$\log(P(\mathbf{X}|\Theta)) = \log \prod_{i=1}^n P(x_i|\Theta) = \sum_{i=1}^n \log \sum_{k=1}^K \alpha_k P(x_i|\theta_k) \quad (6)$$

257 The direct maximization of the log-likelihood function in Eq. (6) is complex and cannot
 258 be found analytically. Usually the maximum likelihood estimation is obtained using the
 259 expectation-maximization (EM) algorithm [Song et al. \(2007\)](#), which learns the distribution
 260 parameters θ from the data, and this is the algorithm implemented in this research for the
 261 inference of the distribution parameters.

262 In general, GMMs represent the probability distributions of the given observations.
 263 Learned GMM distributions can be used to make statistical inferences about the prop-
 264 erties of the given observations. In an unsupervised clustering context, GMM modelling
 265 focuses on grouping data based on a mixture of, possibly multivariate, Gaussian distribu-
 266 tions. This leads to construct clusters which are ellipsoidal, centred at the mean vector,
 267 and with varying geometric features such as volume, shape and orientation determined by
 268 the covariance matrix Σ_k . It is possible to parametrize the covariance matrix through the
 269 eigen-decomposition, which leads to the following definition [Celeux & Govaert \(1995\)](#):

$$\Sigma_k = \lambda_k D_k A_k D_k^T \quad (7)$$

270 where λ_k is a scalar controlling the volume of the ellipsoid, A_k is a diagonal matrix specifying
 271 the shape of the density contours with $\det(A_k)=1$, and D_k is a diagonal matrix which
 272 determines the orientation of the corresponding ellipsoid.

273 The volume, shape and orientation of the covariances can be constrained to be equal
 274 or variable across different groups which leads to the definition of different clusters with

275 different characteristics and shapes as defined in Table 1 and implemented in the `mclust`
 276 package [Scrucca et al. \(2016\)](#).

Table 1: Parametrisation of the covariance matrix Σ_k for multidimensional data [Scrucca et al. \(2016\)](#).

<i>Model</i>	Σ_k	<i>Distribution</i>	<i>Volume</i>	<i>Shape</i>	<i>Orientation</i>
EEI	λI	Spherical	Equal	Equal	-
VII	$\lambda_k I$	Spherical	Variable	Equal	-
EEI	λA	Diagonal	Equal	Equal	Coordinate axes
VEI	$\lambda_k A$	Diagonal	Variable	Equal	Coordinate axes
EVI	λA_k	Diagonal	Equal	Variable	Coordinate axes
VVI	$\lambda_k A_k$	Diagonal	Variable	Variable	Coordinate axes
EEE	$\lambda D A D^T$	Ellipsoidal	Equal	Equal	Equal
EVE	$\lambda D A_k D^T$	Ellipsoidal	Equal	Variable	Equal
VEE	$\lambda_k D A D^T$	Ellipsoidal	Variable	Equal	Equal
VVE	$\lambda_k D A_k D^T$	Ellipsoidal	Variable	Variable	Equal
EEV	$\lambda D_k A D_k^T$	Ellipsoidal	Equal	Equal	Variable
VEV	$\lambda_k D_k A D_k^T$	Ellipsoidal	Variable	Equal	Variable
EVV	$\lambda D_k A_k D_k^T$	Ellipsoidal	Equal	Variable	Variable
VVV	$\lambda_k D_k A_k D_k^T$	Ellipsoidal	Variable	Variable	Variable

277 The selection of the optimal model, *i.e.* number of Gaussian components and the co-
 278 variance parametrization that minimise error, is selected by maximizing the Bayesian In-
 279 formation Criterion (BIC). The BIC is a penalized form of log-likelihood. That is, the
 280 log-likelihood increases with more components and a penalty term is subtracted to compen-
 281 sate for this event. The BIC is defined as follows:

$$BIC_{M,G} = 2\log(L_{M,G}) - m\log(n) \quad (8)$$

282 where $\log(L_{M,G})$ is the maximized log-likelihood for the model M with G components, m is
 283 the number of estimated parameters in the model, and n is the number of observations in
 284 the data. The pair $\{M, G\}$ which maximizes the $BIC_{M,G}$ is selected as the optimal model.

285 Note that the BIC definition in Eq. (8) may be defined as a minimization problem if the
 286 negative log-likelihood and positive penalization term is used. The BIC criteria has been used
 287 because it shows a good compromise between model complexity and accuracy, as compared
 288 with other information criterion metrics such as Akaike information criteria. Penalized forms
 289 of BIC, such as the integrated complete likelihood (ICL), which penalizes BIC through an
 290 entropy term, shows the same performance and model-selection, as also observed in [Vanem
 291 & Brandsæter \(2021\)](#), and accordingly, the simpler BIC definition has been used. ICL seems
 292 to be a preferred solution for unsupervised problems with well-separated clusters [Scrucca
 293 et al. \(2016\)](#).

294 *3.3. Correlation Model*

295 The correlation between the environment model and the turbine model is determined by
 296 the classification of sea-states into different groups and associating the corresponding power
 297 curve to each group. Figure 4 shows the conceptual diagram of the conditional anomaly
 298 detection model, where the $Pr(Environment)$ block shows a random classification of the
 299 different sea-states.

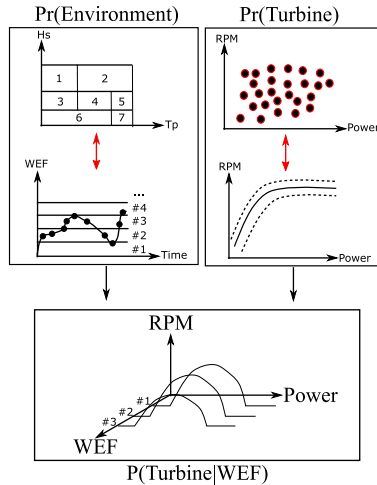


Figure 4: CAD for air turbines operated in the WPP.

300 The environmental model in Figure 4 shows the discretization of the pair $\langle H_s, T_p \rangle$ into the
 301 corresponding WEF sea-state level and characterization of the corresponding power curve.

302 The empirical power curve will be conditioned on the sea-state classification criteria,
 303 $Pr(Turbine|WEF)$, and it will be constructed accordingly. Figure 5 shows this concept by
 304 defining three states, with predefined WEF values to classify signals into one of these states.

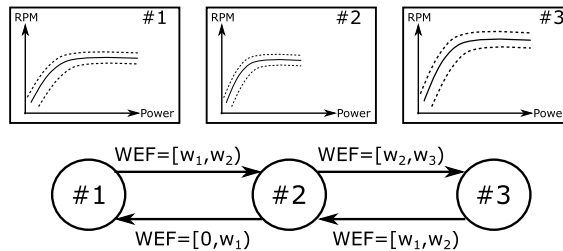


Figure 5: WEF states and corresponding power curve.

305 The transition conditions between different sea-states are deterministic boundary WEF
 306 values. The extension of the framework to include probabilistic transition rates is left for
 307 future work.

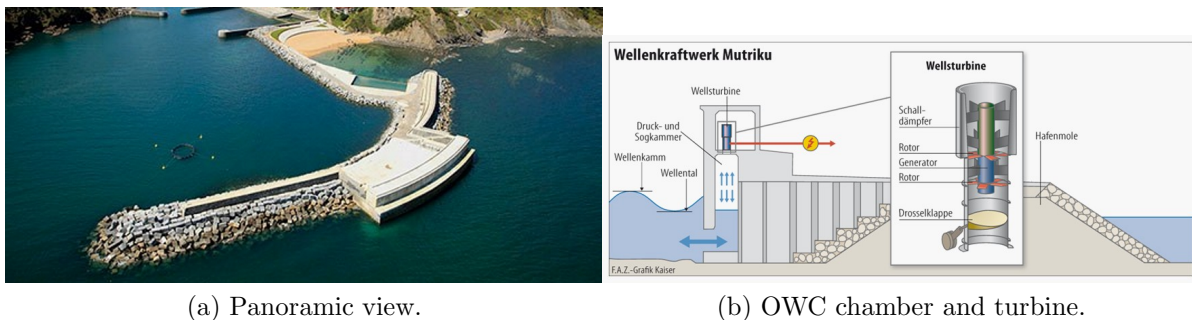
308 **4. Case Study**

309 The approach suggested in Section 3 is tested on the Mutriku WPP located in the Gulf
 310 of Biscay. The WPP is constructed onshore, integrated into a breakwater that protects

311 Mutriku’s fishing harbour, as shown in Figure 6 (a). The WPP is based on the OWC
 312 principle and consists of 16 independent air chambers with their corresponding air-turbine
 313 and electric generator, as illustrated in Figure 6 (b). The OWC technology uses wave energy
 314 to pressurize air in a chamber forcing it through an air turbine. The incoming and outgoing
 315 movement of the sea water within the chamber creates a bidirectional air flow through the
 316 turbine. In turn, the turbine is coupled to a power generator which produces energy.

317 Due to the bi-directional reciprocating air flows generated in the air chambers of OWC
 318 devices, self-rectifying turbines are designed specifically for this application. A number of
 319 self-rectifying turbines have been suggested in the literature Falcao & Gato (2012), being
 320 the Wells turbine the most popular and the one installed in the Mutriku WPP.

321 The 16 air chambers of the Mutriku WPP are equipped with a set of Wells turbines and
 322 an electric generator of 18.5 kW rated power. However, the maximum allowed power of the
 323 generator is extended until 22.5 kW in order to maximise the energy harnessing capabilities
 324 of the WPP. It should be noted that the first and last chambers are disabled and, thus,
 325 only 14 out of 16 chambers are currently operational, resulting in a total rated power of 260
 326 kW (instead of the total capacity of 296 kW) Fäy et al. (2020). In addition to the turbine-
 327 generator set, Figure 6 (b) shows the turbine chamber. Currently, the Biscay Marine Energy
 328 Platform (BIMEP) is the responsible for the operation and maintenance tasks of the plant.



(a) Panoramic view.

(b) OWC chamber and turbine.

Figure 6: Mutriku WPP.

329 From the beginning of the operation of the Mutriku WPP, different degradation and
 330 failure events have been reported for WPP components including air-turbines and electric
 331 generators Lekube et al. (2018), which required unplanned maintenance actions. The lack of
 332 experience in similar systems hampered the development of condition monitoring strategies,
 333 and maintenance actions have been adopted through intuition and expert knowledge.

334 Although grid-connected, the main goal of the Mutriku WPP is promoting the devel-
 335 opment of OWC components, auxiliary systems and control strategies. Therefore, the oper-
 336 ational consequence of unplanned maintenance actions are not as critical as in future
 337 commercial open ocean WPPs. However, the monitored information of the plant operation
 338 can be used to develop health monitoring models that integrate statistical learning strategies
 339 with expert knowledge, and accordingly, assist engineers in the maintenance decision-making
 340 processes of future WPPs. Since the CAD approach suggested includes monitored data from
 341 the environment and the WPP, each datasets are described in the following subsections.

342 4.1. Turbine Operational Data

343 The WPP operates in different modes, automatically identifying the operation mode for
344 each turbine depending of the operation characteristics. In a simplified manner, the WPP
345 starts the operation from shutdown with a *start-up* mode, jumping to *power production*
346 mode once the start-up is completed. Under normal operation, the WPP remains in *power*
347 *production* mode passing through *self-check* mode automatically every 24 hours to verify
348 the correct operation. If the plant is operating at low power or high pressure levels, the
349 WPP enters in *low-power inhibit* or *high-power inhibit* modes, respectively, returning back
350 to *power production* mode when the pressure in the chamber increases in the former case
351 and decreases in the latter. In the case of a serious fault or any other suspicious event,
352 the WPP can be shut down manually so that maintenance operations can be carried out
353 safely. The SCADA system implemented in the Mutriku WPP includes a flag that records
354 the plant operation mode at each instant.

355 The main objective of the developed CAD approach is to identify anomalies that go
356 unnoticed for the described high-level semi-automatic operating system. The *power pro-*
357 *duction* mode is the most relevant operation because it is the energy generation mode, and
358 accordingly, the operation data for this mode is isolated from the rest.

359 For this operation mode, turbines in the Mutriku WPP are controlled combining maximal
360 torque control and flux weakening strategies as shown by Fäy et al. (2020). Maximal torque
361 control is applied when the turbine rotates below the nominal rotational speed, while the
362 flux-weakening strategy comes into play above the nominal rotational speed. Due to this
363 control combination, turbines may operate over its nominal power for a short period of time
364 (up to the previously mentioned 22.5 kW maximum allowed limit). Therefore, the behaviour
365 of the turbines is also conditioned by the control law applied in the turbo-generator, as shown
366 by several studies for different turbines in the context of the Mutriku WPP, e.g. Lekube
367 et al. (2016); Fäy et al. (2018); Otaola et al. (2019); Fäy et al. (2020). As a consequence, it
368 can be assumed that control will have a significant role on the appearance of anomalies.

369 Hence, rotational speed is the variable that affects most in the generated power and, as
370 a consequence, both variables are used in the CAD approach presented in this study. In
371 addition, these two variables are the ones that show the highest correlation among all the
372 monitored mechanical variables. In order to limit the scope of the study the turbine T10 in
373 the Mutriku WPP is studied extracting data for the period 10/09/2019-10/12/2019. This
374 period of time provided the most consistent set of data for the analysis. Figure 7 (a) shows
375 the instantaneous measurements for rotational speed, power, pressure and vibrations from
376 top to bottom, while the correlation among the different variables is shown in Figure 7 (b).

377 4.2. Environmental Data

378 For the context-informed CAD approach, the information about the context is provided
379 by the sea-state conditions through the pair $\langle H_s, T_p \rangle$. These two statistical parameters can
380 be combined for the computation of the WEF [cf. Eq. (1)], which provides the available
381 wave power at a certain location per unit of wave-crest length. Although both T_p and H_s
382 are vital for an accurate resource characterisation, the context information required by the

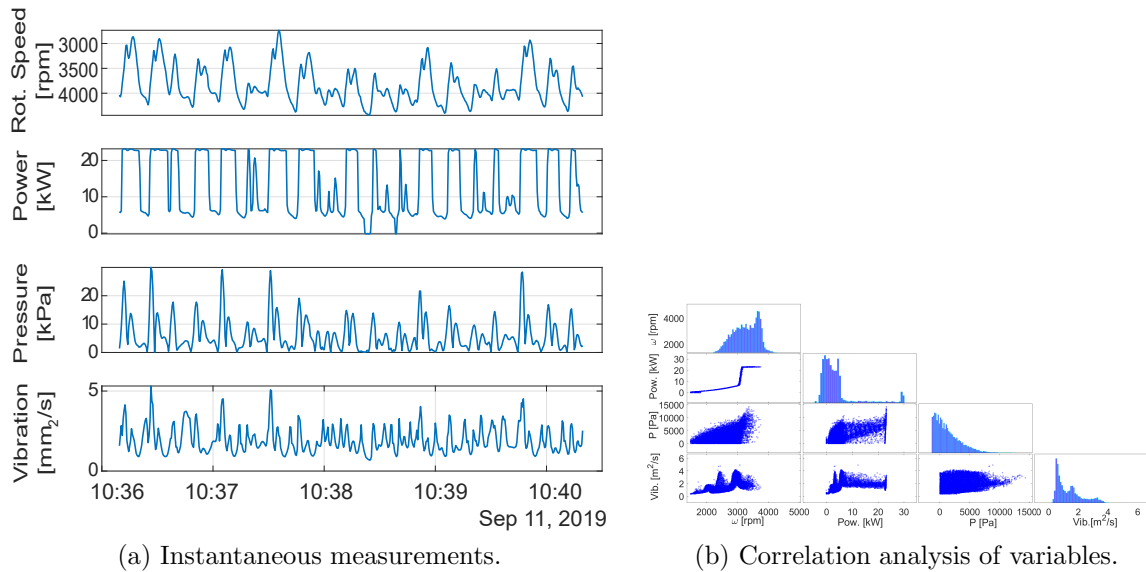


Figure 7: T10 air turbine monitoring.

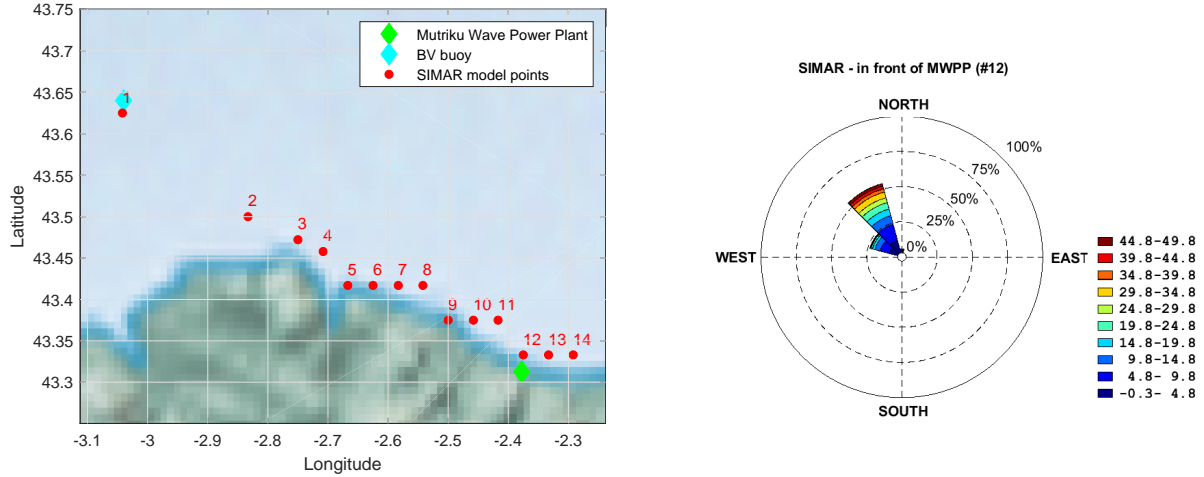
383 CAD approach presented in this study must be synthesised in a single parameter, for which
 384 the WEF is selected.

385 Data on wave climate characteristics at a certain location can be obtained by means of
 386 two main sources: *in-situ* buoy measurements, *e.g.* [Ruggiero et al. \(2010\)](#) and [Mérigaud &](#)
 387 [Ringwood \(2018\)](#), and wave model and re-analysis datasets, *e.g.* [Reguero et al. \(2015\)](#) and
 388 [Ulazia et al. \(2020\)](#). *In-situ* buoy measurements are the most reliable source of data, which
 389 can provide direct measurements of the free-surface elevation or post-processed statistical
 390 parameters, such as T_p and H_s . The former requires a prohibitive on-board data storage
 391 capacity for a relatively small wave-riding buoy and, as a consequence, main oceanographic
 392 agencies provide mean statistical parameters of measured wave data.

393 However, *in-situ* data is not always available, due to geographical or temporal limitations.
 394 Wave model and reanalysis data are highly valuable in these cases, providing data that cover
 395 large geographical areas along various decades. In the present study, wave data from the
 396 SIMAR model is used. SIMAR is an ensemble of modelling metocean data created upon a
 397 high-resolution numerical model by the Spanish Oceanographic Agency Puertos del Estado,
 398 which covers the coast along the Iberian Peninsula between 1958-2020 with a temporal
 399 resolution of 1 hour. It is important, though, that in order to extract solid conclusions,
 400 model and reanalysis datasets should be adequately validated.

401 For this work, data from the SIMAR model in front of the Mutriku WPP is considered.
 402 Since no measurement data is available for this precise location, the validation of the SIMAR
 403 model data is carried out at the closest grid point of the SIMAR model for which *in-situ*
 404 data exists. Figure 8 (a) illustrates the geographical location for the Mutriku WPP, the
 405 Bilbao-Vizcaya (BV) measurement buoy of the Spanish Oceanographic Agency Puertos del
 406 Estado and the different grid points of the SIMAR model along the coast between the BV
 407 buoy and Mutriku WPP. The validation is recently carried out in [Martinez-perurena et al.](#)

408 (2021) between wave data at gridpoint 1 and *in-situ* measurements of the BV buoys and this
 409 validation of the SIMAR model is considered to provide confidence on the model in order
 410 to use the wave data that is closest to the Mutriku WPP at gridpoint 12 in Figure 8 (a).
 411 Figure 8 (b) shows the predominant wave direction in front of the Mutriku WPP.



(a) Mutriku WPP, BV buoy, SIMAR gridpoints. (b) Predominant wave direction of the resource.

Figure 8: Wave resource data from the SIMAR model: (a) model gridpoint location, (b) wave rose.

412 So as to design a conditional anomaly detection model, the environmental data is cate-
 413 gorised according to expert knowledge. Accordingly, the continuous WEF (with a temporal
 414 resolution of 1 hour) is discretised into five main groups. The discretisation criteria is based
 415 on the mean WEF at the Bay of Biscay, which is reported to be around 20 kW/m in different
 416 studies in the literature, *e.g.* [Ulazia et al. \(2017\)](#), resulting in five different categories as
 417 follows:

- 418 ● WEF 1: Very low energetic sea-states: 0-5 kW/m
- 419 ● WEF 2: Low energetic sea-states: 5-15 kW/m
- 420 ● WEF 3: Medium energetic sea-states: 15-25 kW/m
- 421 ● WEF 4: High energetic sea-states: 25-40 kW/m
- 422 ● WEF 5: Very high energetic sea-states: 40+ kW/m

423 Figure 9 illustrates this discretisation comparing the continuous and discrete WEF signals
 424 for the period of time studied in this paper. As a consequence, as described in Figure 5, for
 425 each WEF configuration, the associated performance parameters of the WPP are monitored.
 426 Note that the mapping between sea-states and WPP health states is influenced by the
 427 propagation delay of sea-states that is jointly defined by the physical distance between the
 428 buoy and the WPP, and environmental conditions.

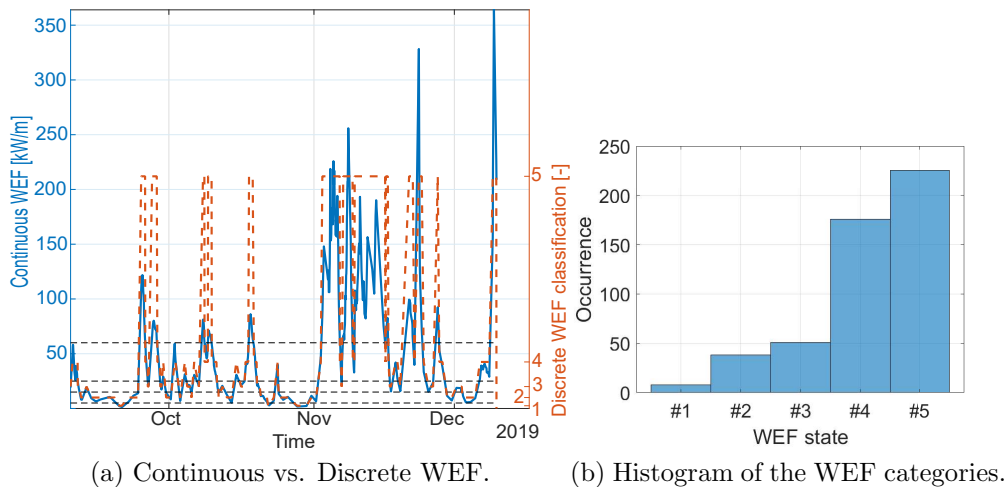


Figure 9: Wave energy flux based discretization of sea-states.

429 The selection of the number of sea-states impacts on the performance of the anomaly
 430 detection model. This is driven by engineering expert knowledge and leads to perform
 431 well in the tested scenario. However, changing the number of categories into less states,
 432 leads to obtaining a model which does not discern between different contextual information
 433 and causes false negatives. In contrast, increasing the number of states, leads to a very
 434 contextually-sensitive model, which flags false positive events.

435 5. Results

436 5.1. Data Pre-processing

437 Following the framework shown in Figure 3, the data preprocessing activity is comprised
 438 of three connected steps. Firstly, invalid data readings with abnormal values are removed so
 439 as to avoid biases in the data, such as out-of-range values and missing data. Subsequently,
 440 original 10 Hz sampled signals are downsampled into 5-minute averages, so as to avoid
 441 false positives with specific wave conditions and ensure the duration of anomalous events
 442 throughout the 5-minute intervals. Figure 10 shows the downsampled signals for generated
 443 power and rotational speed.

444 Finally, data-binning is implemented so as to ease the probabilistic analysis by converting
 445 data more suited for Gaussian components. Namely, the data-binning step counts as the
 446 same value data points differing by low values, and this step smooths the GMM learning
 447 process through the expectation-maximization algorithm avoiding the algorithm to collapse
 448 Song et al. (2007).

449 5.2. Correlation Analysis

450 In order to analyse the correlation between Mutriku WPP variables and sea-state infor-
 451 mation it is necessary to align both datasets. On the one hand, Mutriku WPP variables are
 452 collected through a SCADA system with a sampling rate of 10 Hz. On the other hand, the

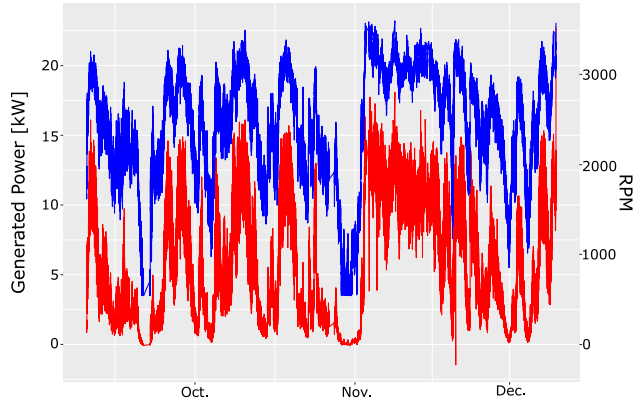


Figure 10: Pre-processed data from 10/09/2019 to 10/12/2019.

453 SIMAR model at the gridpoint #12 in front of the Mutriku WPP provides wave data with
 454 a temporal resolution of 1 hour. Figure 11 shows the evolution of the WEF (in blue) and
 455 the power generation of the Mutriku WPP (in red) for a 1-hour resolution.

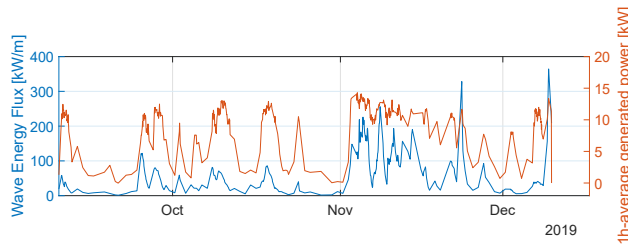


Figure 11: WEF and generated power.

456 In order to demonstrate the temporal alignment of wave resource and WPP datasets,
 457 a cross-correlation analysis is carried out comparing hourly wave data from the SIMAR
 458 model at the gridpoint #12 and the downsampled WPP variables with the same temporal
 459 resolution. The downsampling of the SCADA data to obtain hourly data is performed via
 460 time-integration of the generated energy within one-hour intervals. Figure 12 illustrates the
 461 cross-correlation analysis between the generated power and WEF, where no delay is shown.
 462 It should be noted that this delay is consistent across all the evaluated scenarios.

463 Finally, the correlation among the different WPP variables is studied in order to better
 464 understand the operation of the WPP. The Pearson correlation is low for all the variable
 465 pairs, meaning that the linear relationship between all variable pairs is low. However,
 466 non-linear relationships between some variable pairs are identified. The most relevant rela-
 467 tionship is found between rotational speed and generated power. Figure 2 illustrates this
 468 relationship, where the saturation effect plays a significant role. In addition, negative power
 469 values appear for low-medium rotational speed ranges, which can be attributed to the control
 470 algorithm that prevents the turbine from stopping when wave power is low. Accordingly, the
 471 anomaly detection analysis in this study focuses on rotational speed and generated power
 472 so as to leverage the information of these variables for condition monitoring.

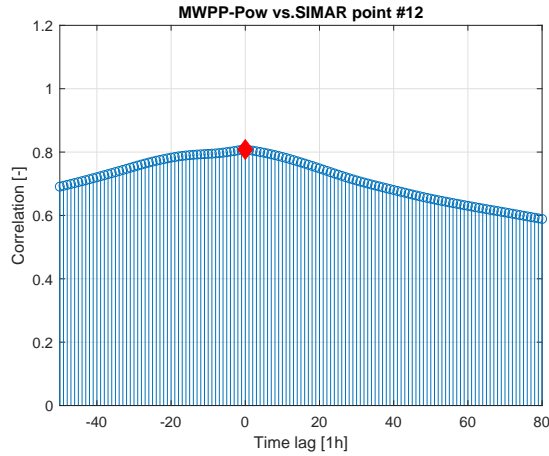


Figure 12: WPP-WEF cross-correlation for the WEF measured at BV buoy.

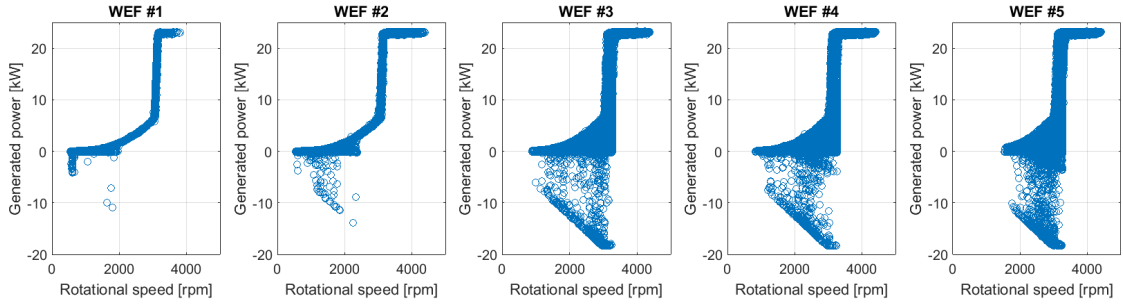
473 The same correlation analysis is also carried out for the five WEF categories and the
 474 corresponding rotational speed and generated power, as shown in Figure 13 (a). Despite
 475 the similarities of the different curves for all the WEF classes, the saturation effect of the
 476 generated power appears to be more significant as wave power increases.

477 5.3. Probabilistic models

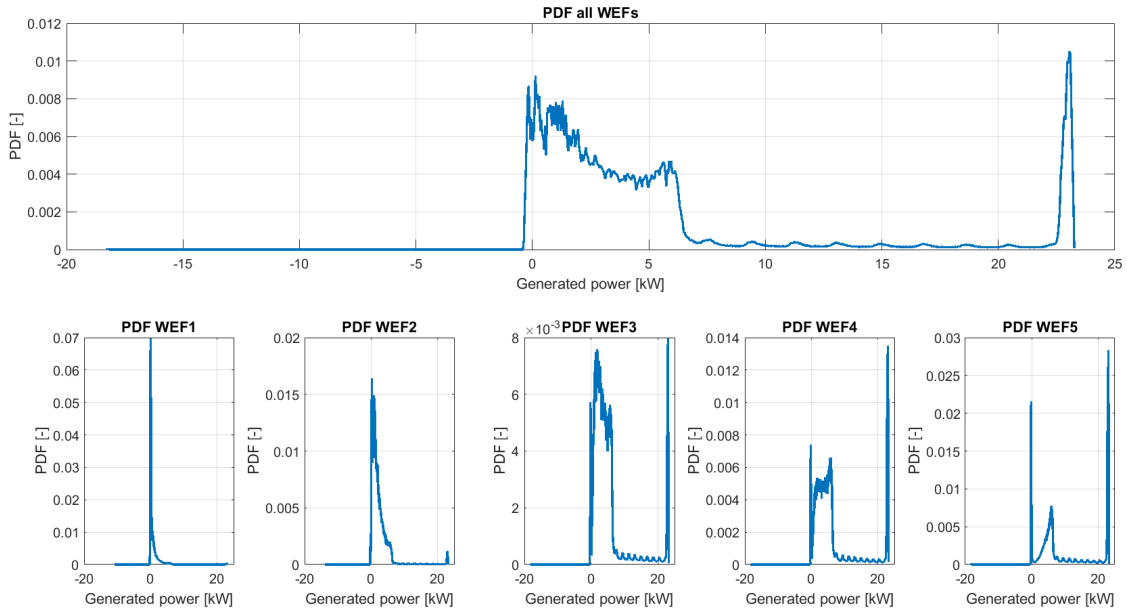
478 Furthermore, a probabilistic descriptive operation analysis of the air turbines has been
 479 carried out in order to understand and characterize the expected operation of the air turbines
 480 as a function of sea-state conditions. Figure 13 (b) shows the different WEF groups and the
 481 associated distributions of the generated power corresponding to each group. It should be
 482 noted that the rated power of each generator is of 18.5 kW, but the plant operation allows
 483 power peaks up to 22.5 kW, which is the maximum allowed power (cf. Section 4.1).

484 It can be observed from Figure 13 (b) that:

- 485 • The overall distribution, including all the WEF classes, shows three main peaks located
 486 at (i) close to 0 kW, (ii) just above 5 kW and (iii) rated power 22.5 kW.
- 487 • The discrete, group-based WEF analysis highlights:
 - 488 – The WEF 1 distribution shows an unimodal distribution with the peak very close
 489 to 0 kW, illustrating a very low power generation.
 - 490 – WEF 2 is similar to WEF 1, but shows a wider and more positively-skewed
 491 distribution, indicating that power generation increases substantially. In addition,
 492 a tiny peak can be observed at the rated power of the turbine, meaning that the
 493 saturation effect has a subtle impact.
 - 494 – WEF 3 and WEF 4 show a very similar bimodal distribution with a broad peak at
 495 low power values and a significant narrow peak at the rated power value. Hence,
 496 the saturation effects is shown to have a relevant impact. The main difference is
 497 the higher relevance of the peak at the rated power in WEF 4.



(a) WEF categories and associated power curves.



(b) WEF categories and associated distributions of WPP performance variables.

Figure 13: Mutriku WPP characterisation for each WEF class.

498 – Finally, WEF 5 shows a clear trimodal distribution with the three characteristic
 499 power generation values located at 0 kW, 5 kW and 22.5 kW.

500 5.4. Anomaly detection

501 In order to design the anomaly detection model of the air turbines, firstly, indepen-
 502 dent probabilistic operation models are designed fitted to different sea-state groups. The
 503 probabilistic operation models are based on empiric power curves that capture the depen-
 504 dency between the generated power and rotational speed. Figure 2 shows the empiric power
 505 curve of the WPP computed with the monitored dataset without separation into different
 506 sea-states.

507 From the available three months dataset, one month has been used to train the probabilis-
 508 tic models, and the subsequent two months have been used for testing the trained models.
 509 For the sake of manageability and in order to reduce false positives, available datasets are

510 downsampled into 5-minutes averaged data. Averaging datasets reduces the otherwise pro-
 511 hibitive computational burden, smooths the monitored variables and removes instantaneous
 512 anomalous events. Note that wave data is also upsampled accordingly by means of a linear
 513 interpolation method.

514 Figures 14-18 shows the downsampled empiric power curves for the different WEF groups
 515 corresponding to the training dataset. Differences between Figure 13 (a) and Figures 14-18
 516 arise, precisely, due to the downsampling.

517 As for the parameter-tuning process of the GMM models, for each power curve in Fig-
 518 ures 14-18, different GMM models with 14 different covariates (cf. Table 1), and varying
 519 number of GMM components [cf. Eq. (5)] have been fitted. The parameter tuning of each
 520 GMM model has been done using the expectation-maximization algorithm (cf. Section 3).

521 For the fitted GMM models, their corresponding BIC values are computed so as to select
 522 the GMM model that maximizes likelihood and minimizes model-complexity [cf. Eq. (8)].
 523 For each WEF range, the optimal GMM is selected from the tested models, and the selected
 524 GMM models represent the expected normal operation of the WPP within the given WEF
 525 region.

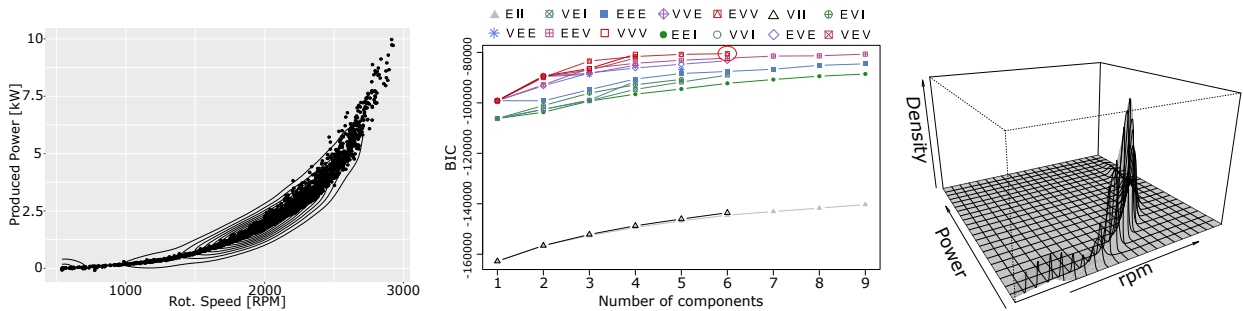


Figure 14: WEF 1: empiric power curve, BIC curves, optimal GMM (6 components, BIC=-80492.11, EVV).

526 A particularity of the lowest-energetic sea-state WEF 1 in Figure 14 is that the rotational
 527 speed never drops below 500 rpm, meaning that the turbine consumes energy from the grid
 528 in order to prevent the turbine from stopping. Thus, the turbine is effectively running on
 529 idle, which allows for a more efficient restart.

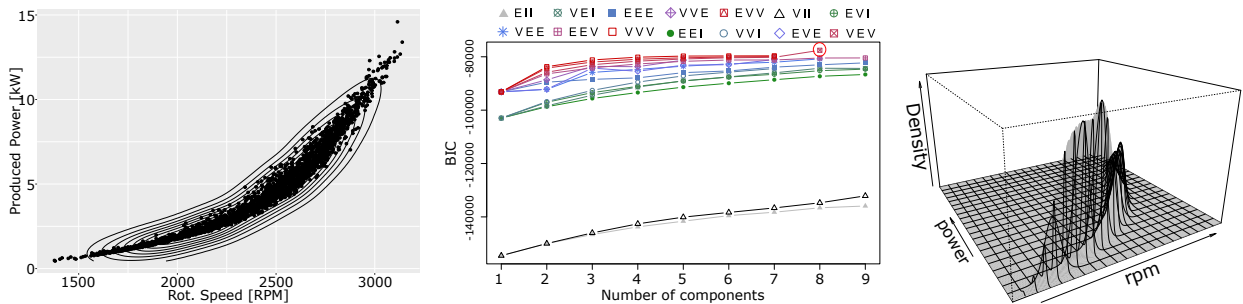


Figure 15: WEF 2: empiric power curve, BIC curves, optimal GMM (8 components, BIC=-77567.86, VEV).

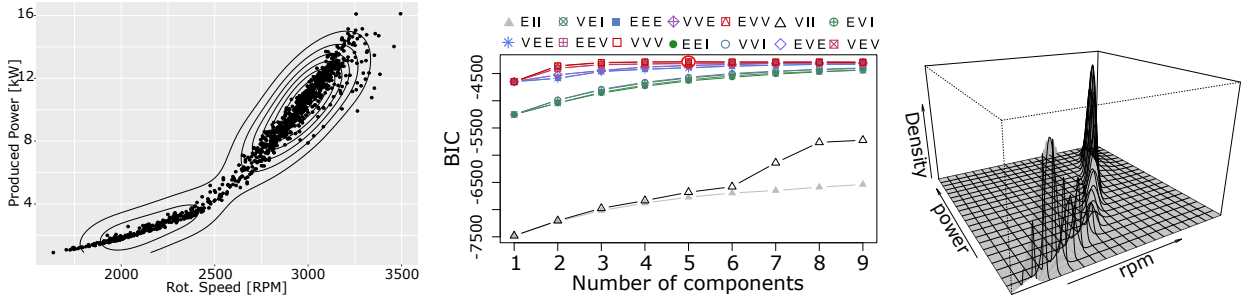


Figure 16: WEF 3: empiric power curve, BIC curves, optimal GMM (5 components, BIC=-42830.23, VVV).

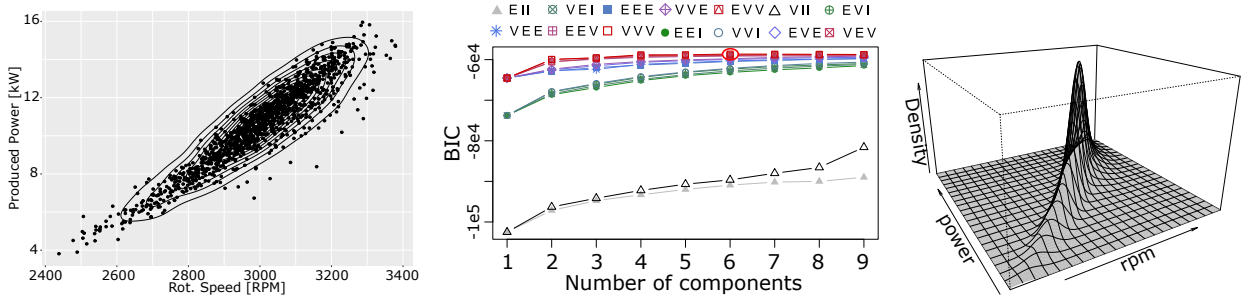


Figure 17: WEF 4: empiric power curve, BIC curves, optimal GMM (6 components, BIC=-58626.75, VVV).

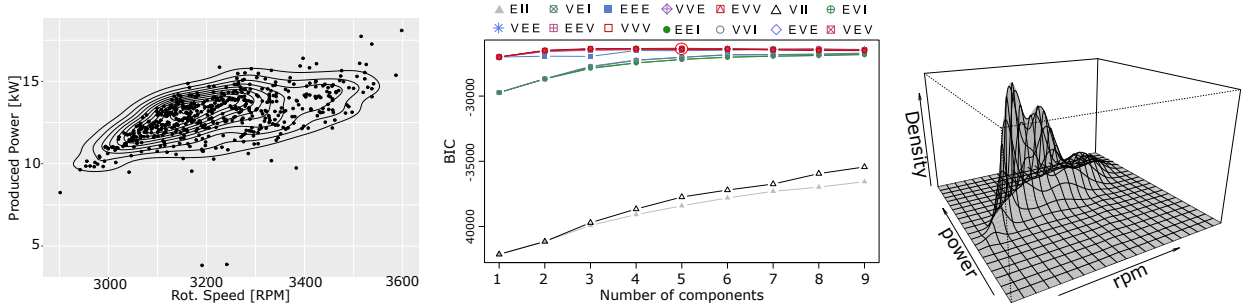


Figure 18: WEF 5: empiric power curve, BIC curves, optimal GMM (5 components, BIC=-26331.96, EVV).

530 It can be observed from the power curves in Figures 14-18 that the generated power and
 531 rotational speed of the different power curves increase from low-energetic sea-states (cf. WEF
 532 1, Figure 14), to high-energetic sea-states (cf. WEF 5, Figure 18). Accordingly, probabilistic
 533 regions have been assigned to each WEF region defined by the fitted GMM, which reflects
 534 the likely expected operation conditions, given the specific sea-state conditions.

535 In parallel, for comparison purposes, the empirical power curve and the GMM have
 536 been also fitted for the case without division into sea-states. Figure 19 shows the empirical
 537 distribution, BIC curves and the optimal GMM model.

538 From Figure 19, it can be observed that the assigned likelihood values for the value pair
 539 power and rotational speed, are different from the likelihood values assigned in Figures 14-18
 540 to the different value pairs of power and rotational speed. As it will be shown, this will have
 541 a direct impact on the performance of the conditional anomaly detection model when it

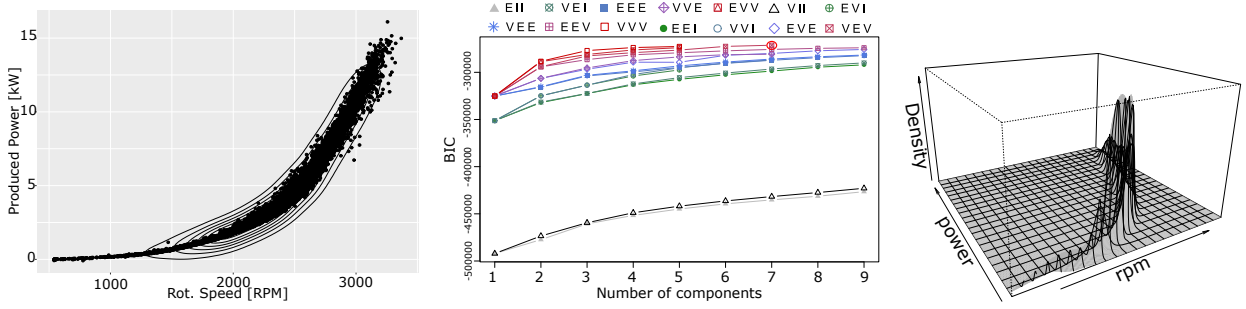


Figure 19: No-States: empiric power curve, BIC curves, optimal GMM (7 components, BIC=-271283.8, VEV).

542 is informed about different sea-states, and when it ignores the information of different sea
 543 states.

544 Subsequently, after learning the GMM models, for testing purposes, depending on the
 545 observed sea-state condition, the corresponding anomaly detection model is activated to
 546 detect anomalies. In this way, each independent anomaly detection model focuses on iden-
 547 tifying deviations from expected operation conditions for the considered WEF group. The
 548 main implementation steps of the anomaly detection process are defined as follows:

- 549 1. Read pair $\langle H_s, T_p \rangle$
- 550 2. Calculate WEF and identify sea-state group
- 551 3. Estimate likelihood of the reading via GMM of the corresponding WEF
- 552 4. Evaluate log-likelihood value and determine anomaly

553 Figure 20 shows anomaly detection results for the different energetic sea-states along with
 554 the model without classification into sea-states. The vertical axis has been transformed into
 555 log-likelihood scale for anomaly representation purposes Song et al. (2007). The lower the
 556 log-likelihood, the more likely to be an anomalous event, because it represents an unlikely
 557 situation. Three different threshold levels have been represented so as to show the effect of
 558 different boundaries on triggering anomalous events: (a) -12.5, (b) -25 and (c) -50 in the
 559 log-scale.

560 From Figure 20 it can be observed that there is a variation in the sea states across the
 561 analysed period along with the obtained log-likelihood values. It can be also seen the inferred
 562 log-likelihood value differences between the classification into different sea-states (WEF 1-5)
 563 and no-classification of sea-states (no states). This is expected from the fitted GMM models
 564 for WEF 1-5 (Figures 14-18) and the GMM with no-states (Figure 19).

565 As for the different failure threshold levels, for example, for the threshold level (c), the
 566 no-states configuration identifies three anomalies, while the state-based anomaly detection
 567 matches only with one of them corresponding to the sea-state WEF 2. The subsequent
 568 analysis will elaborate further the results shown in Figure 20 focusing on the analysis of the
 569 events (#1)-(#2) and (#3)-(#4) that correspond, respectively, to the sea states WEF 5 and
 570 WEF 2.

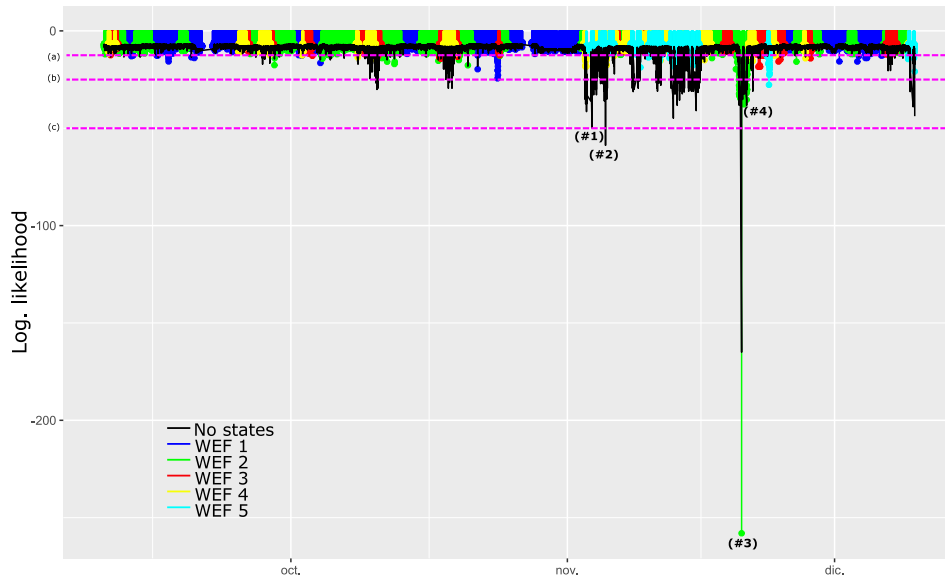


Figure 20: Anomaly detection results.

571 *5.4.1. WEF 2 events*

572 Figure 21 shows anomaly detection results for sea-state 2 (WEF 2) along with the cor-
 573 responding log-likelihood.

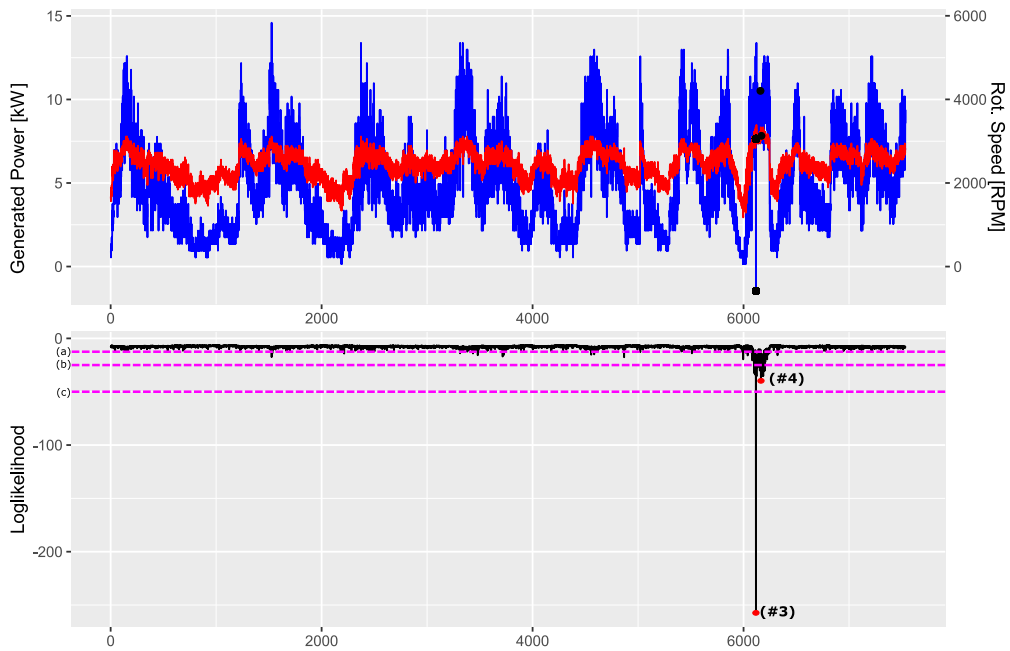


Figure 21: Anomaly detection results for WEF 2.

574 Figure 21 highlights the potential anomalous events with the corresponding log-likelihood.
 575 The lower the likelihood, the lower the occurrence probability. Focusing on two events with

576 the lowest occurrence likelihood, highlighted with markers in Figure 21, it can be observed
 577 that one is below the most restrictive threshold (c), *i.e.* event (#3), and the other is below
 578 the threshold (b), *i.e.* event (#4).

579 Figure 22 shows the expanded time-series of the generated power and rotational speed,
 580 corresponding to the anomalous events.

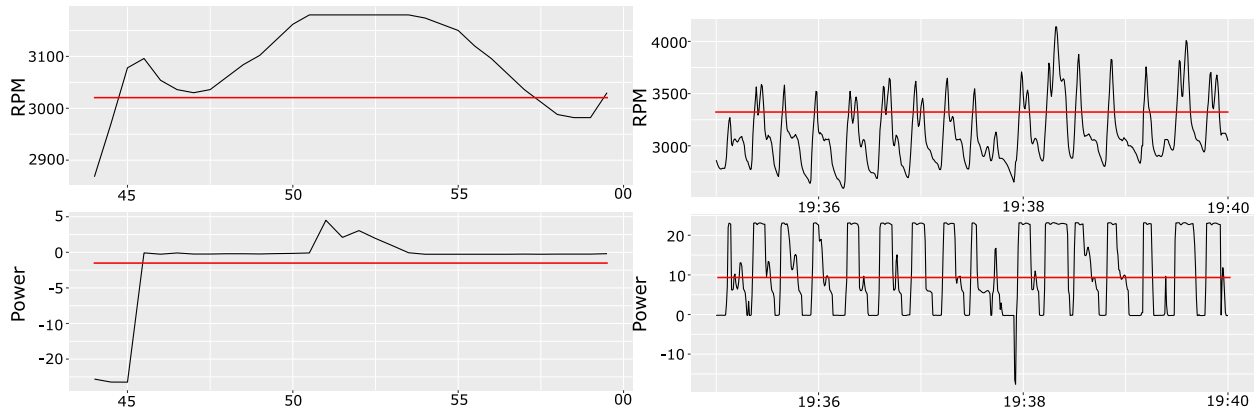


Figure 22: (a) Event (#3) located at 2019-11-20, 13:30; (b) Event (#4) located at 2019-11-20, 19:40.

581 From Figure 22(a), it can be observed that the averaged power and rotational speed
 582 values of the event (#3) are -1.46 kW and 3058.3 rpm, respectively. Comparing these values
 583 with the learned GMM of the WEF 2 in Figure 15, it can be inferred that the occurrence
 584 likelihood is zero. It can be also noticed in Figure 22(a) that there are only 16 second
 585 samples out of the 5-minutes interval, *i.e.* the rest of samples in this interval are zero. This
 586 is not flagged as an anomalous plant operation, but an incorrect sensor reading, as confirmed
 587 by plant operation experts.

588 Figure 22(b) shows the corresponding expanded 5-minutes time-series for the event (#4).
 589 It can be observed that the averaged power and rotational speed values are 9.77 kW and
 590 3335.09 rpm. Comparing these values with the learned GMM of the WEF 2 in Figure 15,
 591 it can be inferred that the occurrence likelihood is not as low as in the previous case, but
 592 corresponds to an unlikely event. This is due to the decrease in produced power (see the
 593 expected power in Figure 15). This is not a real anomaly and therefore threshold (c) would
 594 classify it correctly, while threshold (a) and (b) would misclassify it.

595 Figure 23 shows the anomaly detection results for the model that does not consider
 596 separation of sea-states.

597 Focusing on the three events below the lowest threshold in Figure 23, it can be observed
 598 that the lowest likelihood event (#3) matches with the anomaly flagged by the WEF 2
 599 sea-state GMM model located at 2019-11-20 at 13:30 (cf. Figure 21). As for the event
 600 (#4), it can be observed that according to the threshold (c) it would classify it correctly
 601 and thresholds (a) and (b) would misclassify the event.

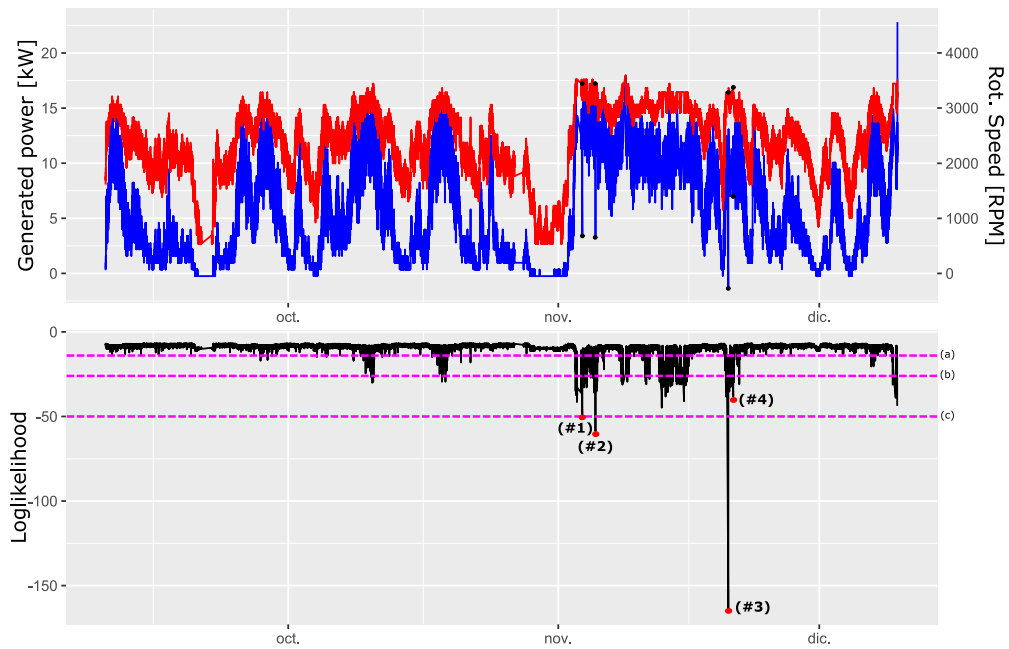


Figure 23: Anomaly detection results without separation into WEF states.

602 *5.4.2. WEF 5 events*

603 There are two additional events associated with the WEF 5 sea-state around first two
 604 weeks of November (cf. Figure 25) flagged as anomalies by the model without separation
 605 into WEF states. Focusing on the event (#1) located at 2019-11-03 at 18:35 Figure 24(a)
 606 shows the expanded 5-minutes time series for power and rotational speed.

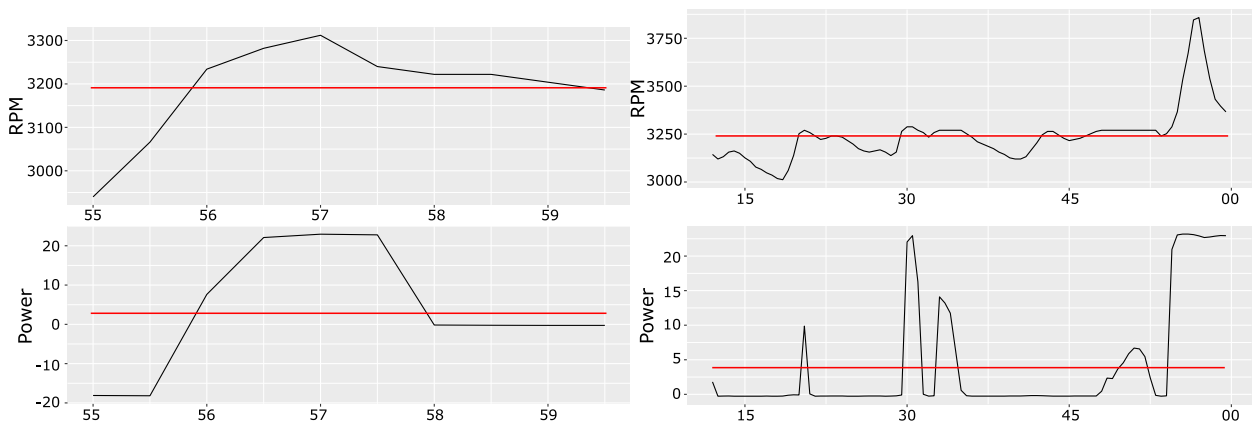


Figure 24: (a) Event (#1) located at 2019-11-03, 18:35; (b) Event (#2) located at 2019-11-05, 06:50.

607 The mean values for power and rotational speed in Figure 24(a) are 3.82 kW and 3190.8
 608 rpm, respectively. Looking at the GMM of the model without states in Figure 19, it can be
 609 observed that the likelihood of this event is low, and this is why the model without states
 610 classifies it as an anomaly. The duration of the event is of 5 seconds out of the 5-minutes

611 interval, which again means that the remainder of readings are zero.

612 In contrast, focusing on the model inferred from WEF 5 sea-state (cf. Figure 18) it can
 613 be seen that there is room for low energy generation. Figure 25 shows individual WEF 5
 614 anomaly detection results.

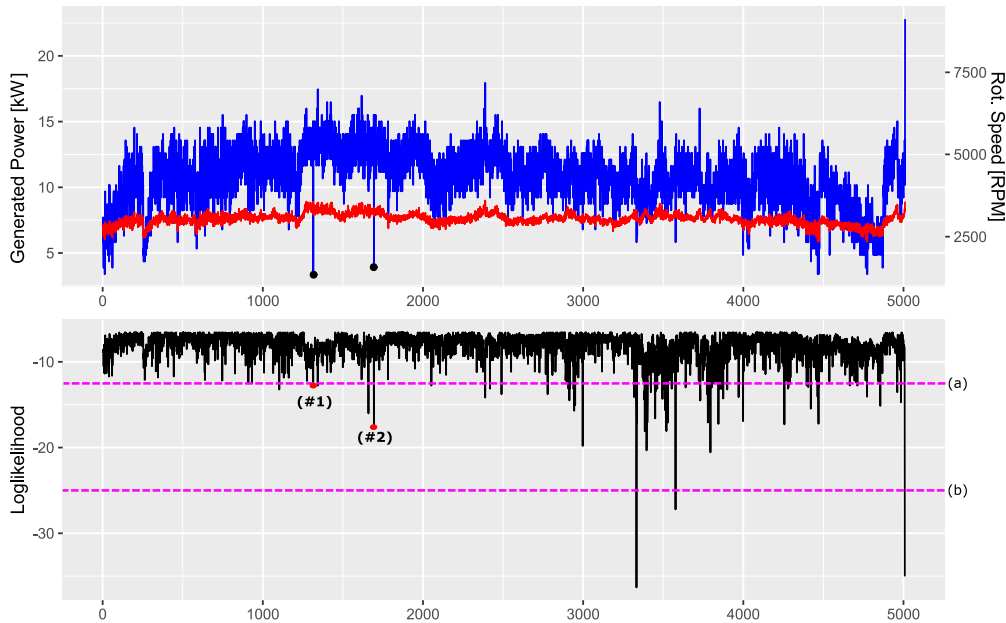


Figure 25: Anomaly detection results for WEF 5.

615 Therefore, event (#1) is flagged as a false positive event by the model without states,
 616 and it is classified correctly for the GMM of the WEF 5, except for the threshold (a).

617 Focusing on the event (#2) located at 2019-11-05 at 06:50 (cf. Figure 23), Figure 24(b)
 618 shows the expanded 5-minutes time series for power and rotational speed. The mean values
 619 for power and rotational speed are 4.11 kW and 3241.37 rpm, respectively. The duration of
 620 the event is of 1 minute, out of 5 minutes.

621 Again, analysing the GMM of the model without states in Figure 19, it can be observed
 622 that the likelihood of this point is low, and this is why it is regarded as an anomaly by the
 623 model without states. In contrast, focusing on the model inferred from WEF 5 sea-state
 624 (Figure 18), it can be seen that there is room for low energy generation assigning a higher
 625 likelihood compared with the model without states (but still small).

626 Therefore, event #2, classified as an anomaly by the model without states, is a false
 627 positive event and this is captured correctly with the model with states, except for the most
 628 restrictive threshold (a).

629 Table 2 displays the obtained results for the different anomaly detection models including
 630 models with and without WEF states and the analysed threshold levels. Additionally, it
 631 also shows the performance statistics of the different anomaly detection models.

632 It can be observed that for the threshold (c) the proposed state-based anomaly detection
 633 model obtains the best performance. For the same threshold, the model without states
 634 generates false positive events that affect the accuracy of the classifier. For the threshold

Table 2: Summary of anomaly detection results and performance statistics.

Events	Threshold					
	(c)		(b)		(a)	
	States	No-states	States	No-states	States	No-states
Event #1	TN	FP	TN	FP	FP	FP
Event #2	TN	FP	TN	FP	FP	FP
Event #3	TP	TP	TP	TP	TP	TP
Event #4	TN	TN	FP	FP	FP	FP
Accuracy	100%	50%	75%	25%	25%	25%
TNR	100%	33,3%	66,6%	0%	0%	0%
TPR	100%	100%	100%	100%	100%	100%
FPR	0%	50%	25%	75%	75%	75%

¹ **Legend:** True Positive (TP), True Negative (TN), False Positive (FP), False Negative (FN)

² $TPR = \frac{TP}{TP+FN}$; $TNR = \frac{TN}{TN+FP}$; $FPR = \frac{FP}{TN+FP}$; $Accuracy = \frac{TP+TN}{TP+TN+FP+FN}$

635 level (b), the performance of both models decreases and for the most restrictive threshold
 636 (a) both models generate false positive events due to the adopted threshold level.

637 This lead us to draw two main conclusions. The separation of sea-states enables the
 638 rational discrimination of expected characteristic power curves given the corresponding sea-
 639 states. In contrast, if the whole dataset is considered without considering sea-states, the
 640 learned probabilistic distributions are WEF-agnostic and they are prone to misclassifying
 641 WPP states as erroneous due to the lack of sea-state information.

642 6. Discussion

643 Although the promising results are shown in this paper, before drawing definitive con-
 644 clusions further work is necessary, contrasting the methodology for other time-periods and
 645 turbines. The identification of the most problematic sea-states requires a verified methodol-
 646 ogy and a significantly larger dataset (a few years of operation) that covers different resource
 647 conditions and operation modes. In order to transit towards a scenario where this identifi-
 648 cation will be possible, some future lines for the improvement of the present approach are
 649 suggested here.

650 Threshold definition without expert knowledge is a challenging task. In some cases, a
 651 physical magnitude can be turned into a threshold value. If that is not the case, it may
 652 occur that it can be determined by evaluating the probability of occurrence of events. In
 653 this research, the effect of different thresholds on different anomalies has been analysed
 654 showing that it plays an important role in decision-making. It is possible to extend this
 655 work by inferring dynamic thresholds from an statistical analysis, such as Bayesian and
 656 Neyman-Pearson hypothesis testing. This will be addressed in future research.

657 The analysed signals in this work have been post-processed by downsampling them to
 658 five minutes average signals. That is, the duration of each point event in the case study is
 659 of five minutes. Therefore, if an anomalous event persists for this period, it is considered a

660 non-intermittent event. This was a trade-off decision between complexity and duration of
661 the events. It may have been possible to evaluate the effect of different sampling rates on
662 the anomaly detection approach.

663 In this research, the identification of sea-states is based on expert knowledge because
664 it is hypothesized that it would be beneficial for the classification of sea-states. The limits
665 between energetic sea-states are deterministic, and therefore, there is room for converting this
666 classification into a data-driven probabilistic approach. Future work will consider the use of
667 trivariate statistical models and copula concepts [Jiang et al. \(2021\)](#) to evaluate data-driven
668 sea-states modelling concepts and compare with expert-based categorization of sea-states.

669 **7. Conclusions**

670 This paper presents a context-informed unsupervised conditional anomaly detection ap-
671 proach for air turbines operated in wave power plants (WPP). The approach has been tested
672 and evaluated in the Mutriku WPP. The proposed approach has been focused on the use of
673 power curves and energetic sea-states formalized through an ensemble of Gaussian Mixture
674 models and expert knowledge.

675 Results obtained from the application to the Mutriku WPP show the potential of the
676 proposed approach to detect air turbine anomalies through explicit consideration of different
677 sea-states along with power curves. It has been shown that without consideration of sea-
678 state information the anomaly detection model is prone to flag false positive events and the
679 integration of sea-state information aids in the discrimination of anomaly events.

680 This is part of an ongoing research and authors' plan to extend the anomaly detection
681 approach in different directions including the data-driven inference of anomaly detection
682 thresholds and data-driven identification of sea-states.

683 Future activities within the prognostics and health management (PHM) framework will
684 focus on the development of diagnostics and prognostics approaches for the WPP compo-
685 nents.

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