

Investigation of diffusive and optical properties of vapour-air mixtures: The benefits of interferometry

V. Shevchenko^a, A. Mialdun^b, V. Yasnou^b, Y. V. Lyulin^a, H. Ouerdane^a,
V. Shevtsova^{c,d}

^a*Center for Energy Science and Technology, Skolkovo Institute of Science and Technology,
3 Nobel Street, 121205 Moscow, Russia*

^b*Microgravity Research Centre, CP-165/62, Université libre de Bruxelles (ULB), av. F. D.
Roosevelt 50, B-1050, Brussels, Belgium*

^c*Basque Foundation for Science, Bilbao, Spain*

^d*Mechanical and Manufacturing Department, Mondragon Goi Eskola Politeknikoa
(MGEP), Loramendi 4, Apdo. 23, 20500 Mondragon, Spain*

Abstract

While interferometry has been widely used for diffusion measurements in liquid mixtures, it was hardly applied so far to vapour-gas mixtures. The present work aims to bridge this gap. Using an improved Mach-Zehnder interferometer, we investigate the evaporation of acetone and HFE-7100 in ambient air. Our observations build on complete evaporation of a thin liquid layer in a cell with open end, at ambient temperature varying between 283.15 and 313.15 K. Monitoring the evolution of the refractive index change allows us to determine the evaporation rate and vapour-in-air diffusion coefficients. The spatial distribution of the refractive index reveals that the purely diffusive mode of transport is perturbed at both ends of the cell. Interferometric images facilitate isolating these regions, determining the true diffusion path, and hence, the correct diffusion coefficients. Besides, we illustrate the possibility of calculating the optical contrast factors, which we find in excellent agreement with current experiments.

Keywords: Interferometry, Vapor-in-air diffusion coefficient, Vapor optical properties, acetone, HFE-7100

1. Introduction

Evaporation from free liquid surfaces is a heat transfer mode that plays a crucial role in chemical engineering, biology, and practical applications such as, e.g., humidification of air, spray cooling, drying, and delivery of medical aerosols to name a few. The actual needs for the experimental assessment of the gases diffusive properties thus range from very practical purposes such as defense – diffusion of warfare gases or their simulants in air [1], to purely academic ones, e.g. an experimental support of the Chapman-Enskog theory [2]. It is also worth noting that in the electronic industry, the current intensive development of efficient cooling systems and heat pumps based on liquid–vapor–liquid phase transitions [3, 4] triggers a renewed interest for the diffusive properties of vapour-gas mixtures, as vapor transport through a gas phase appears to be a limiting factor.

Diffusion in a given system is the slow transport of matter, spreading from one region to another, caused by concentration gradients. It is a complex process that depends also on the thermodynamic conditions, notably pressure and temperature, and chemical concentration and phase of the environment where it occurs. The diffusion coefficient of vapor in gas is one of the important parameters used in mathematical modelling and numerical simulations of heat and mass transfer through the gas-liquid interfaces [5, 6, 7]. To predict precisely the global evaporation rate from the liquid surface into gas, one may use the values of the diffusion coefficients given in benchmark databases [8]. However, the determination of the global evaporation rate averaged over a certain time period and measured in many experiments is not enough to understand well all fundamental aspects in the evaporation process from the free surface.

Non-uniform evaporation from gas-liquid interfaces, which takes place in most actual evaporative systems, can change flow patterns within a liquid volume. For instance, the Marangoni effect due to a non-uniform evaporation providing thermocapillary stresses on the liquid surface is a reason of the complex convection in liquid layers [9]. In some cases the thermocapillary effects may

31 cause the breakdown of liquid film [10]. It is evident that the cross-influence
32 study of convection and evaporation should be considered in terms of the lo-
33 cal evaporation rate from the gas-liquid interfaces. The determination of the
34 local evaporation rates bears a particular importance in the study of heat and
35 mass transfer in the contact line zone of the liquid droplets [11]. Considering
36 more specifically the evaporation from surfaces of liquid droplets [12, 13, 14],
37 bridges [15] and layers [16, 17], either in a stationary or moving gaseous en-
38 vironment, the evaporation rate is limited by the vapor diffusion into the gas.
39 Fick's laws for steady-state and time-dependent regimes, are widely used to de-
40 termine the evaporation rate from gas-liquid interface into gas phase, for which
41 the knowledge of the diffusion coefficients as function of the vapor temperature
42 is needed. However, lack of systematic measured data of their diffusive and opti-
43 cal properties as functions of temperature in gases, in the benchmark databases,
44 hinders progress.

45 Diffusion coefficients can be obtained by various experimental methods such
46 as, e.g., Laser induced fluorescence (PLIF) [18] or Fourier transform infrared
47 spectrometry (FTIR) [19]. These optical techniques can be used for measur-
48 ing local evaporation rates or vapor concentrations over gas-liquid interfaces,
49 but they do not show sufficient resolution for the analysis of vapour concentra-
50 tion gradients in the gas phase. Measurement of the vapor concentration and
51 local evaporation rate require the knowledge of the vapor-gas mixture refrac-
52 tive index variation with vapor concentration, i.e. the so-called optical contrast
53 factor. Interferometry is another optical measurement technique, which is sen-
54 sitive enough to quantify the amount of vapor in gas [20, 21, 22], and hence
55 which is well-suited for our purpose. In fact, application of digital interferome-
56 try was found to be an optimal solution for measuring the local distribution of
57 the evaporation rate along the liquid surface from a direct measurement of the
58 vapour concentration gradient normal to the gas-liquid interface [22]; and it is
59 particularly successful for substances featuring high molar mass and significant
60 partial vapor pressure. In addition, optical digital interferometry is widely and
61 successfully used for measuring diffusion and thermal diffusion coefficients in

62 liquid mixtures [23, 24, 25]

63 Despite a number of new and competing techniques to measure the binary
64 gas diffusivities, the Stefan tube method, introduced in the end of 19th century,
65 is still very popular due to its simplistic arrangement. An overview of the
66 method can be found in [26], where condensed but detail-rich description of
67 the technique is supplemented with a deep analysis of possible error sources.
68 Some practical problems have been discussed already in [26], and extensively
69 studied later on [27, 28, 29, 30]. Nevertheless, the method is in continuous use,
70 and even is modified to cover wider use-cases, e.g. when the data is needed
71 at temperatures exceeding boiling point [31], although, the use of non-volatile
72 solvent may also introduce a bias in the result [32]. The first attempts to apply
73 interferometry to the Stefan tube date back to the 1960s [20, 21], with the data
74 treatment being limited at the time to manual fringe tracking method.

75 When using an evaporation-diffusion tube for measuring diffusion coeffi-
76 cients, experiments rely on the monitoring the rate of evaporating liquid loss,
77 either by visual tracking of the liquid level [27, 32], or, gravimetrically [33, 34].
78 In the present study, even if a somewhat similar geometry is used, the observa-
79 tion is built on the complete evaporation of a thin liquid layer placed in a cell
80 with open end designed for optical measurements.

81 Two often-used liquids with a very different volatility were selected for tests:
82 HFE-7100 and acetone. HFE-7100 is a low volatile liquid, and since it has low
83 surface tension and low viscosity, it penetrates into tight spaces in delicate elec-
84 tronic equipment, which makes it suitable for thorough and complete cleaning.
85 HFE-7100 is also widely used as heat-transfer liquid in electronics. Acetone, on
86 the other hand, is a highly volatile liquid that is well characterised and therefore
87 suitable for validating the experimental approach.

88 In the present study, Mach-Zehnder interferometry with improved stability
89 combined with modern digital interferogram processing based on 2D Fourier
90 transform, is applied to measure the diffusion coefficient and optical properties
91 of selected vapors in air. Considering HFE-7100 and acetone, we present and
92 discuss the evaporation rates, refractive indices and optical contrast factors, as

93 well as vapor diffusion coefficients in air. The temperature dependence of the
94 measured quantities is investigated over a 30 K range, starting from 283.15 K.

95 The goal of the article is two-fold: on the one hand, to demonstrate the
96 value of digital interferometry for the measurement of the diffusive and optical
97 properties of vapour-air mixtures and, on the other hand, to provide precise
98 measurement data of these properties for acetone and HFE-7100 vapours in air.
99 The article is organized as follows. In Section 2, we describe the experimental
100 setup and procedure, with a focus on the optical technique. The experimental
101 results are presented and discussed in Section 3. Concluding remarks are given in
102 Section 4. Additional data and technical details are given in the accompanying
103 Supplemental Information.

104 **2. Experimental**

105 *2.1. Materials*

106 Two liquids were used in the experiments: acetone of the purity $\geq 99.8\%$
107 (for analysis, EMSURE[®] ACS, ISO, Reag. Ph Eur), supplied by Merck, and
108 HFE-7100 (Novec[™] 7100 Engineered Fluid), of the purity $\geq 99.5\%$, purchased
109 from Sigma-Aldrich. Both liquids were used without further purification. The
110 main characteristics of the liquids are listed in Table 1.

111 *2.2. Interferometer*

112 In the present work, a Mach-Zehnder interferometer is used to measure the
113 vapor concentration inside the rectangular cell. The experimental setup, consist-
114 ing of the optical cell, interferometer, video acquisition and thermostabilizing
115 systems, is depicted in Fig. 1. A coherent light beam is generated by a red
116 diode-pumped solid-state laser RLTMRL-671 of Roithner LaserTechnik (wave-
117 length $\lambda = 671$ nm, TEM₀₀ beam profile, and output power ranging from 1
118 to 200 mW). The beam is expanded by a spatial filter, then passes through a
119 collimating lens and at the exit its diameter covers the entire area of the cell.
120 Then, the beam splitter (BS1) divides the beam into two parts of equal intensity

Table 1: Properties of the liquids used in the experiments on evaporation. All the properties are given for the reference temperature of 298.15 K.

	Acetone	HFE-7100
Chemical name	Propan-2-one	Methoxy-nonafluorobutane
CAS No.	67-64-1	163702-08-7, 163702-07-6
Chemical formula	C_3H_6O	$C_4F_9OCH_3$
Molar mass M , $g\ mol^{-1}$	58.08	250
Density ρ , $kg\ m^{-3}$	784.24	1481.57
Thermal expansion β_T , $10^{-3}\ K^{-1}$	1.56	1.53
Thermal conductivity k , $W\ m^{-1}\ K^{-1}$	0.159	0.068

121 (reference and objective). The objective beam traverses the experimental cell
122 while the reference beam bypasses the cell in the open air. Changes in both
123 temperature and concentration due to phase change in the cell contribute to
124 the spatial distribution of the refractive index in the objective beam. Then,
125 the two beams are redirected by mirrors M1 and M2 to spatially join at the
126 second beam splitter (BS2). The appropriate tilting angle and width of inter-
127 ference fringes can be adjusted by varying the inclination angle of the mirrors
128 M1, M2. Large aperture optics was used for monitoring a cell height up to
129 45-48 mm: 2" diameter mirrors and beam splitters. The resulting interference
130 pattern is captured by the CCD camera of JAI CV-M4+CL with the resolution
131 of 1280×1024 pixels and frame rate up to 24 fps. A Thorlabs MVL50HS lens
132 (focal length 50 mm and $f/\# = 0.95$) was chosen as the objective camera lens to
133 ensure the appropriate magnification. Overall, the imaging system provided a
134 picture of the cell with the scale of $42.8\ \mu m/\text{pixel}$.

135 All the components are fastened to an optical bench plate of $900 \times 600\ mm^2$,
136 and the entire interferometer is enclosed in a box made of insulating material
137 3 cm thick. An air-to-air heating/cooling assembly of Laird (part no. AA-040-

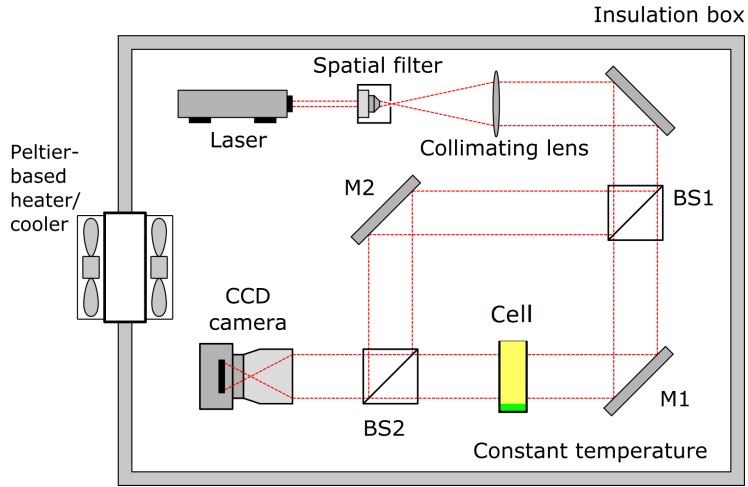


Figure 1: Schematic of the Mach-Zehnder interferometer used to measure the vapor concentration.

138 12-22-00-00) has been incorporated into one of the box walls. The assembly was
 139 driven by dedicated PID controller of Laird (part no. PR-59). The tempera-
 140 ture feedback to the controller was implemented by a calibrated precision NTC
 141 thermistor, which has been in permanent contact with a metallic holder of the
 142 test cell.

143 Such an arrangement has solved three problems at once. First, it provides
 144 a constant and monitored temperature of the ambient gas around the cell with
 145 ability to regulate this temperature in a certain range. Second, it maintains
 146 the interferometer at constant temperature throughout the experiment, thereby
 147 eliminating its possible temperature drift. Third, the fan of the inner heat-sink
 148 of the heating/cooling assembly ensures an airflow around the cell, fast enough
 149 for removing the vapor reaching the open top of the cell. This airflow can cause
 150 a slight jitter of the fringe contrast. However, after the numerical reconstruction
 151 of the interferograms, we did not observe any notable rise in the optical phase
 152 noise.

153 The Hellma cells, being specially designed for optical measurements, features
 154 high-quality glass walls with very well characterized dimensions. The commer-

155 cially available standard absorption cell of Hellma, QS 100-10-40, fits well to
 156 the size of all our optical elements. Characteristic sizes of the cell, critical for
 157 the study, are indicated in Fig. 2.

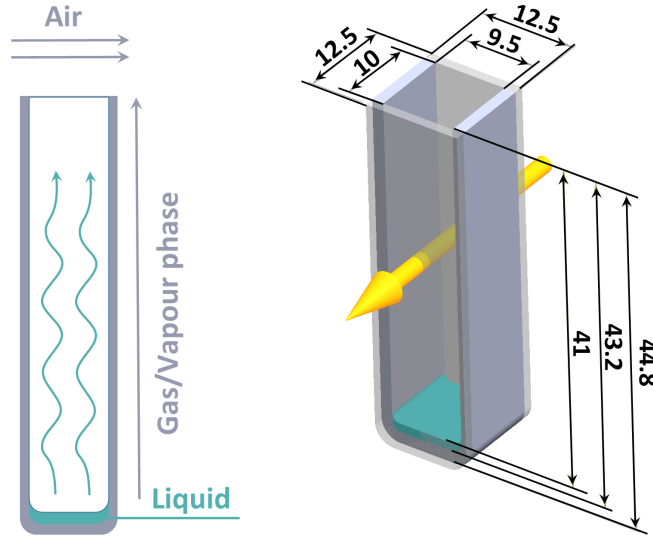


Figure 2: Schematic of the experimental cell and its 3D drawing with indication of all critical sizes. The arrow indicates the direction of the laser beam.

158 *2.3. Experimental procedure*

159 A typical approach, widely used in previous works [27, 32] is to monitor the
 160 descending level of the interface during evaporation, from which the evaporation
 161 rate and vapor diffusion coefficient are derived. To ensure accurate measure-
 162 ments, it is necessary to fill the diffusion tube with a significant amount of
 163 liquid. A moving interface makes the process unsteady and requires appropri-
 164 ate adaptation of the analytical solution describing the problem. In our case
 165 with a relatively short diffusion tube, the procedure was modified to keep the
 166 diffusion path as long as possible.

167 To do so, a small amount of liquid is injected so that the initial height of
 168 the liquid layer is much smaller than the total cell height. Liquid is carefully
 169 injected by a Hamilton syringe, Gastight® #1725 LT (volume 250 μl , scale

170 division $5\ \mu\text{l}$), that allows an accurate control of the liquid sample volume. The
171 volume was always constant and equal to $0.20 \pm 0.002\ \text{ml}$. The resulting height
172 of the liquid in the cuvette varied slightly depending on the temperature of
173 the experiment and was $\approx 2.2\ \text{mm}$. The meniscus was formed after the filling
174 process at the contact line between the liquid-gas interface and the cell walls and
175 made a small part of the gas phase adjacent to the interface invisible to optics,
176 which, however, did not disrupt data processing. Although the presence of a
177 meniscus could potentially affect the outcome, we did not expect a noticeable
178 impact, so, we neglected it. Since the vapor flux was measured by estimating
179 the total time of the complete sample evaporation, this approach requires a tiny
180 amount of liquid for measurement. The efficiency of the chosen approach was
181 well confirmed in the very first tests (see the beginning of Sect. 3 for details).

182 The smallness of the sample is especially important as the liquid evaporates
183 into a closed box. The volume of the box is rather large comparing with the
184 cell's volume (80 l vs. 4 ml), which makes it possible to neglect the residual vapor
185 concentration in the surrounding air. Nevertheless, after the end of each experi-
186 mental run, the box was carefully vented with the conditioned air of laboratory
187 to eliminate the vapor leftover from a previous experiment.

188 *2.4. Optical phase extraction*

189 We are interested in the variation of the refractive index caused by evapora-
190 tion. In optical interferometry, an interferogram with useful optical information
191 is always processed relative to a reference one taken before the refractive index
192 changes. This reference image is afterwards subtracted from each of the sub-
193 sequent images to identify the characteristics of interest. The reference image
194 is the first recorded interferogram when the liquid is not injected yet. In this
195 case, the beam passes only through air and walls of the cell. The reference
196 image includes three contributions in a phase shift: optical elements along the
197 beam path, non-uniform air temperature and the temperature distribution in
198 glass walls (if any). The following images are acquired after liquid injection
199 (Fig. 3(a)). Its evaporation leads to a change in the refractive index over the

200 experimental cell. These images contain two more important contributions: the
201 temperature and the concentration distributions in the gas phase. When all
202 interferograms are recorded, the image processing starts. We follow the previ-
203 ously developed procedure of image processing [35, 36]. Each grey-scale image
204 is read by a Python script as a 2D array of pixels of different intensity, from 0 to
205 255 (a value of 0 represents black and a value of 255 represents white). Fringes
206 in the images are well distinguished; a magnified fringe pattern is shown in
207 Fig. 3(b). Fringe spacing is about 4-5 pixels. An example of the initial intensity
208 distribution is shown in Fig. 3(c) over the horizontal line.

209 2D Fourier transform is applied to all the images to get an optical phase
210 at each pixel. This procedure is equally applied for the reference and objective
211 images. A typical intensity distribution in Fourier space is shown in Fig. 3(d) on
212 which one can distinguish bright spots. Spots represent the first-order intensity
213 peaks while zero-order one is placed in the corners of the images. To proceed,
214 the position of the peaks in the Fourier space should be changed. The 2D
215 Fourier transform output is rearranged by moving the spectrum on f_{x0} toward
216 the origin of Fourier domain (Fig. 3(e)). The zeroth-order peak $I(f_x, f_z)$ gives
217 the amplitude information, which is not of interest to us, while the first-order
218 peaks $C(f_x - f_{x0}, f_z)$ and $C^*(f_x + f_{x0}, f_x)$ carry equal information about the
219 phase shift - see Fig. 3(e). The zeroth-order peak is right in the center and
220 the first-order peaks are located on the sides (Fig. 3(f)). In the ideal case,
221 each peak would be represented by one point. But because of inaccuracies in
222 the interferometer, such as tension in optical elements and non-ideally adjusted
223 tilting angle, peaks are broadened in some area. To discard the zeroth-order
224 peak, a dedicated filter was made for this region using an inverse Gaussian. After
225 application of the filter to the original image, the zeroth-order peak disappears.
226 Then, any peak of the first order can be used for further processing, and the
227 second one should be deleted. The remaining first-order peak should be placed
228 in the center of the image before proceeding. For this, a new filter is created
229 and applied to all the images, and only one peak remains in them, as shown in
230 Fig. 3(g).

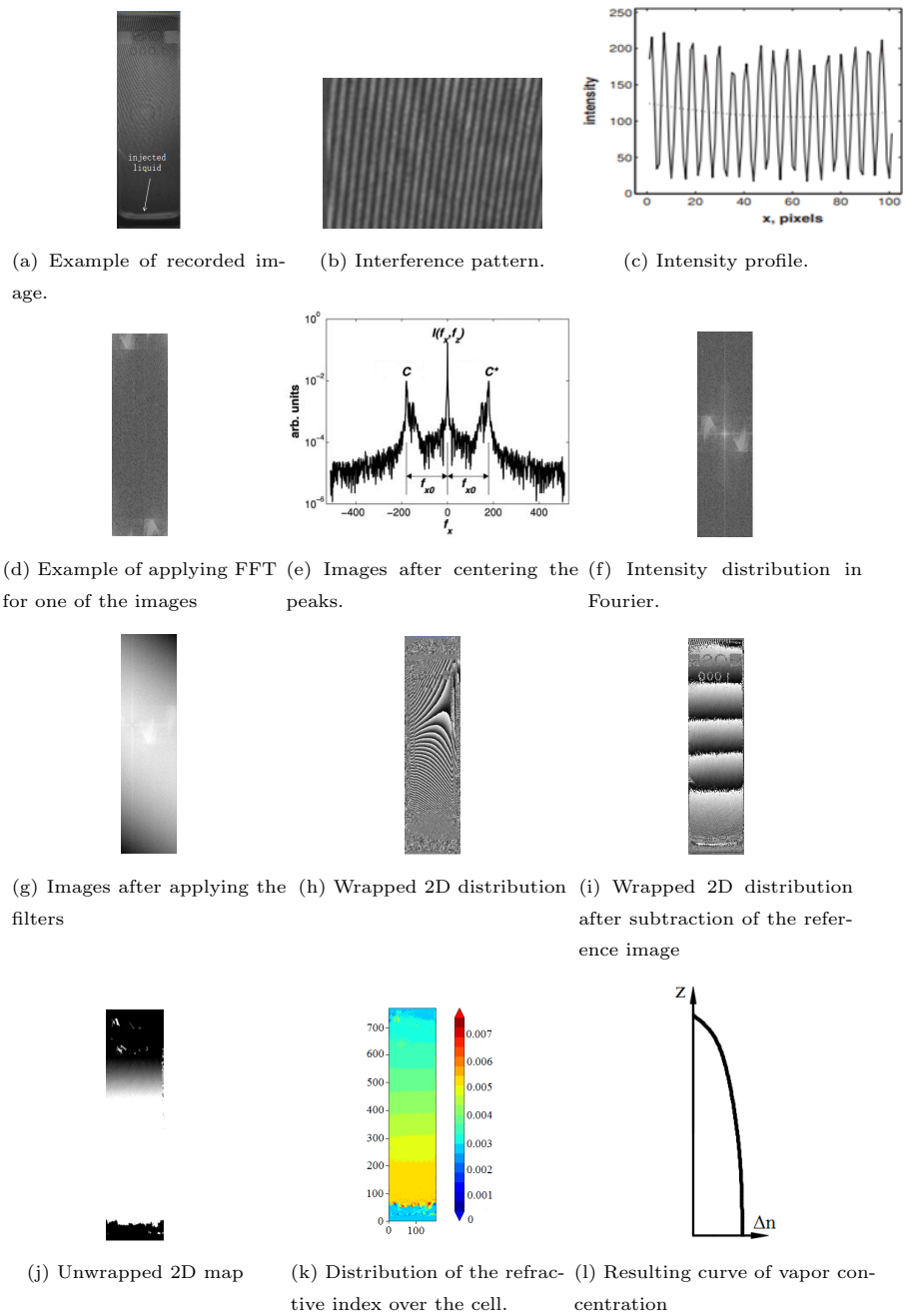


Figure 3: Steps of the optical phase extraction.

231 In the next step, an inverse FFT is applied to the pre-processed reference and
 232 objective images. Then the reference image is subtracted from all the objective
 233 images to get rid of non-informative contributions. After this step, it is even
 234 possible to recognize by eyes the optical phase change due to the concentration
 235 and temperature variations as seen in Fig. 3(i). But the phase is wrapped, which
 236 means that it belongs to the range $(-\pi; \pi)$ after inverse FFT. The following step
 237 is the application of the phase unwrapping algorithm. The algorithm searches
 238 and eliminates the discontinuities which are represented by 2π phase jumps
 239 between two nearby pixels. The unwrapped phase map is shown in Fig. 3(j).

The obtained optical phase variation $\Delta\varphi$ is recalculated into the refractive
 index as

$$\Delta n = \Delta\varphi \frac{\lambda}{2\pi L_{opt}} \quad (1)$$

240 where λ is the wavelength of the probing laser beam, and $L_{opt} = 10.0$ mm is the
 241 path-length of the light beam inside the Stefan cell.

242 The final step in the optical information analysis is the elimination of the
 243 absolute value ambiguity, as the phase and refractive index maps obtained by the
 244 above way are always relative. This is done presuming that at the open end of
 245 the tube the vapor concentration is always zero, and temperature disturbances
 246 are absent there. Then, all vertical profiles are normalized in a way to anchor
 247 the value at the very top pixel to zero.

248 **3. Results and discussion**

249 *3.1. Diffusive regimes observed during the course of experiment*

250 Using interferometric measurements, we have identified three temporal regimes
 251 of vapor diffusion, occurring at different times of the experiment and with differ-
 252 ent duration. These regimes are clearly distinguished on the plot of the temporal
 253 evolution of the full refractive index difference Δn , shown in Fig. 4 and detailed
 254 in Fig. 5. Figure 5 presents the distribution of the refractive index with the
 255 cell height. Since the obtained two-dimensional refractive index maps change
 256 mainly in the vertical direction, we select for further analysis one representative

257 profile in the vertical direction, which is obtained by averaging over a strip of
 258 10 pixels wide along the central axis.

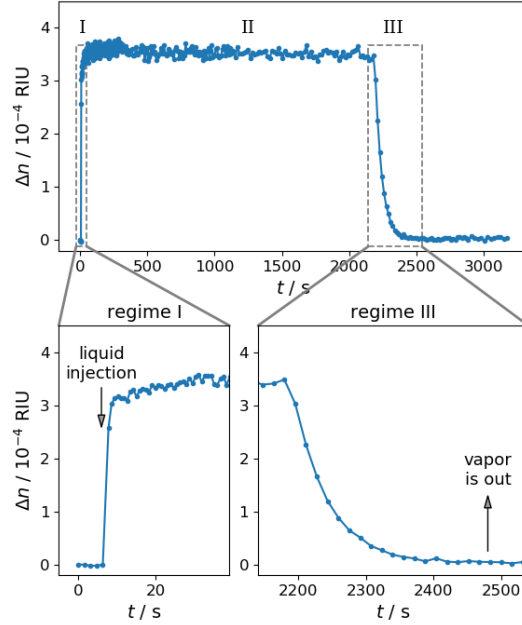


Figure 4: Distinct regimes appearing in the course of a typical experiment. Two callouts show the regimes I and III with different time scales. The plotted case corresponds to evaporation of acetone at the ambient temperature of $T = 313.15$ K.

259 Regime I corresponds to the time interval between the start of the liquid
 260 injection into the cell and establishing of a steady vapor concentration profile.
 261 As may be seen in the callout to Fig. 4 corresponding to regime I, it lasts a
 262 very short time, i.e. a few seconds. During this regime the vapor concentration
 263 (corresponding to the refractive index shown) almost immediately reaches the
 264 saturation level at the interface, and then the vapor travels to the open end of
 265 the cell until a steady profile is established. The distribution of the refractive
 266 index profiles $n(z)$ over the cell height at different times is shown in Fig. 5. In

267 total, the establishment of a steady profile takes less than 20 s.

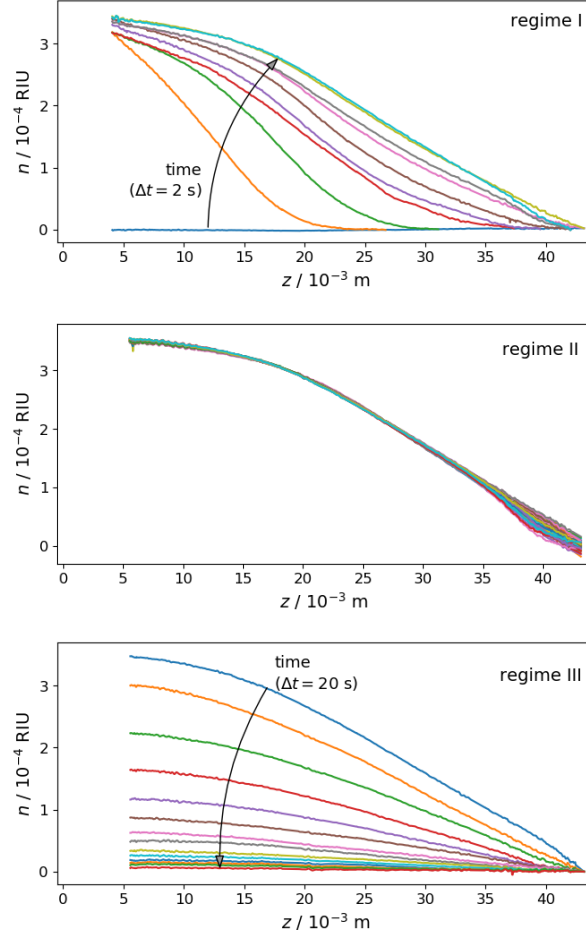


Figure 5: Time evolution of the refractive index profiles for three regimes distinguished in Fig. 4 in experiments with acetone at $T=313.1$ K. For each point in time, one representative profile in the vertical direction is displayed, which is obtained by averaging over a strip of 10 pixels wide along the central axis. Note that variations in the refractive index directly correspond to the behavior of the vapor concentration.

268 Regime II starts when both the total refractive index difference Δn and the
 269 refractive index profiles $n(z)$ are practically frozen. Figure 5b shows that all
 270 the $n(z)$ profiles obtained at different times merge into one curve, except for the

271 region near the top of the cell. This regime, characterized by an almost perfect
 272 steady state, ends up with an abrupt drop of Δn , which logically corresponds to
 273 the complete evaporation of the liquid. A noticeable presence of Δn oscillations
 274 during this regime can be seen in Fig. 4. However, Fig. 5 demonstrates that
 275 the region in which these fluctuations occur is limited, and located at the very
 276 top of the cell. The reason for the existence of such localized fluctuations is
 277 discussed in detail in section 3.4.2.

278 Regime III begins at the moment when there is no more liquid to feed a
 279 steady vapor distribution inside the cell, and it ends when the vapor completely
 280 leaves the cell and the refractive index distribution thus returns to its original
 281 state. The slow decrease in the level of the refractive index profiles with time
 282 (vapor concentration) in this regime can be traced in Fig. 5c.

283 While it is possible to use each of these regimes for the extraction of the
 284 diffusion coefficient, we chose the regime II for at least two reasons. The steady
 285 profiles allow not only fitting them to an existing analytic solution to determine
 286 the vapor diffusion coefficient, but also to evaluate the optical properties of the
 287 vapor-air mixture, provided that the saturation vapor pressure is known.

288 *3.2. Evaluation of evaporation rate and interfacial temperature*

289 *3.2.1. Evaporation rate*

290 A typical approach to measuring the evaporation rate in the configuration
 291 of the Stefan tube is to monitor the lowering rate of the liquid-vapor interface.
 292 Here, we use a different way to measure the evaporation rate, namely, by es-
 293 timating the time required for the complete evaporation of the injected liquid.
 294 This time interval corresponds to the duration of the regime II, and can be
 295 accurately extracted from the experimental record, e.g., see Fig. 4.

The measured evaporation time t allows the calculation of the evaporation
 rate

$$N_v = \frac{\tilde{n}}{t \cdot S} \quad (2)$$

296 where $\tilde{n} = \rho V / M_v$ is the number of moles of the evaporating liquid, ρ is its
 297 density, M_v its molar mass, $V = 0.20$ ml is the volume of injected liquid sample.

298 The evaporating surface is assumed to be plain, without menisci, and measures
 299 $S = 9.25 \times 10.0 \text{ mm}^2$.

300 Measurements were carried out with two liquids in the temperature range
 301 from 283.13 to 313.15 K and the results are summarized in Table 2. The same
 302 values of evaporation rate, but expressed in mass units instead of moles, are
 303 given in Table S2 in Supplementary Material.

Table 2: Temperature T/K ; number of moles of the evaporated liquid $\tilde{n}/10^{-3} \text{ mol}$; optically-measured total time of evaporation t/s ; and evaporation rate $N_v/10^{-3} \text{ mol s}^{-1} \text{ m}^{-2}$ for acetone and HFE-7100.

T	\tilde{n}	t	N_v
<i>Acetone</i>			
283.15	2.76	8400	3.55
288.15	2.74	6500	4.56
293.15	2.72	4800	6.13
298.15	2.70	3900	7.48
303.15	2.68	3000	9.66
308.15	2.66	2600	11.1
313.15	2.64	2150	13.3
<i>HFE-7100</i>			
283.15	1.21	12500	1.05
288.15	1.20	9900	1.31
293.15	1.19	7700	1.67
298.15	1.19	6300	2.04
303.15	1.18	5050	2.53
308.15	1.17	4000	3.16
313.15	1.16	3050	4.11

For both liquids, the temperature dependence of the evaporation rate is well

described by second-order polynomials

$$\begin{aligned}
 N_v(\text{Ace}) &= 7.64 \cdot 10^{-3} + 3.28 \cdot 10^{-4}(T - T_0) + 3.31 \cdot 10^{-6}(T - T_0)^2 \\
 N_v(\text{HFE}) &= 2.03 \cdot 10^{-3} + 9.81 \cdot 10^{-5}(T - T_0) + 2.40 \cdot 10^{-6}(T - T_0)^2 \quad (3)
 \end{aligned}$$

304 with the reference temperature $T_0 = 298.15$ K. The region of validity of the given
 305 correlations is ± 15 K around the reference point. The convenience of this form
 306 of polynomial representation is that the free term gives directly the evaporation
 307 rate at the reference temperature.

308 The experimental data points and correlations are presented in Fig. 6.

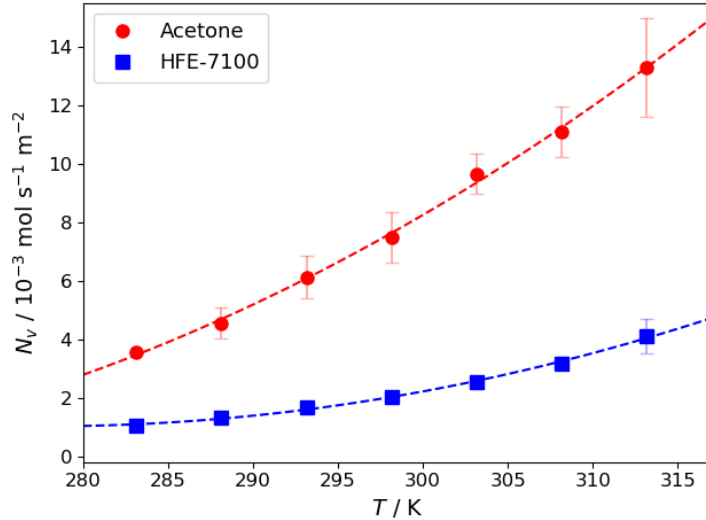


Figure 6: Dependence of the experimental evaporation rate on temperature for acetone and HFE-7100. The error bars are standard deviations.

309 The evaporation rate in both liquids increases by about four times with
 310 an increase in temperature by $\Delta T = 30$ K. In addition, Fig. 6 indicates that
 311 acetone has a larger rate of the increase with temperature compared to HFE-
 312 7100. Each presented data point is obtained by averaging over two to four tests
 313 and the error bars are also shown in Fig. 6. Among the three parameters in
 314 Eq. (2), the evaporation time t exhibits the largest scattering, reaching upper

315 limit 7% for HFE-7100 and of 12% for acetone. Since the errors in defining \tilde{n}
316 and S are much less, the error specific to t , is transmitted to the error of N_v .

317 3.2.2. *Temperature drop on the gas-liquid interface*

318 Evaporation induces a cooling of the liquid–gas interface. In order to calcu-
319 late the temperature drop at the interface caused by evaporation, we consider
320 the problem of stationary conductive heat transfer along the cell. Assuming adi-
321 abatic sidewalls, heat propagates in a one-dimensional manner from the bottom
322 and top of the cell (both are at the ambient temperature) towards the interface,
323 which acts as a heat sink due to evaporation. Our experimental approach al-
324 lows to precisely calculate the heat absorbed by the evaporating interface. The
325 evaporation rate was characterized in the previous section (see 3.2.1), but for
326 the thermal properties the mass units are used, i.e., $N_v = m/t \cdot S$. Here m
327 is the mass of the evaporated substance which is known, since its volume is
328 precisely dosed. With the data on latent heat of vaporization available in the
329 literature [37, 38], the evaporative heat flux can be estimated as $Q = \Delta_v H \cdot N_v$.
330 After determining the evaporative heat loss, the problem can be solved analyti-
331 cally with respect to the interface temperature (see details in the Supplementary
332 Material).

333 All the results related to the temperature drop for the experiments per-
334 formed are summarized in Table S2 of the supplement, and here we suggest
335 some conclusions. First, the effect is not large; in all the cases the temperature
336 drop is limited to the range $0.9 < |\Delta T_{calc}| < 5.9$ K, and, as expected, it is more
337 pronounced at higher temperatures. Second, the thermal effect of acetone is
338 noticeably higher than that of HFE-7100. Thus, in experiments with acetone,
339 one can expect large disturbances of a thermal nature.

340 3.3. *Optical properties of vapor–air mixtures*

The interferometry measures the combined effect of concentration and tem-
perature. For the given wavelength, the variation of the refractive index Δn is

caused by the variations of the vapor concentration Δx_v , and the vapor temperature ΔT

$$\Delta n = \left(\frac{\partial n}{\partial x}\right)_{p,T} \Delta x_v + \left(\frac{\partial n}{\partial T}\right)_{p,x} \Delta T \quad (4)$$

341 The relation includes the so-called *optical contrast factors*, $\left(\frac{\partial n}{\partial x}\right)_{p,T}$ and $\left(\frac{\partial n}{\partial T}\right)_{p,x}$,
 342 which are the concentration- and temperature-related factors, respectively. These
 343 contrast factors are the characteristics of the medium, and can be independently
 344 measured or calculated. In what follows, for ease of notations, we omit the sub-
 345 scripts indicating the conditions at which the contrast factors are obtained.

346 The applied approach is aimed not only at obtaining the vapor concentration,
 347 but also at comparing the measured Δn_{exp} with its analogue Δn_{calc} , calculated
 348 mostly on the basis of external information. This allows to estimate the accuracy
 349 of theoretical predictions of the optical properties of the vapor-air mixtures as
 350 well as consistency of the experimental measurements.

351 We begin with an example of evaluation of the experimental and of calculated
 352 optical properties of vapor-air mixtures such as Δn used in this work. Figures 4
 353 and 5 show that for acetone at $T = 313.15$ K the total refractive index difference
 354 between the liquid interface and the open top is roughly $\Delta n_{exp} = n_{z=b} - n_{z=H} \approx$
 355 $3.5 \cdot 10^{-4}$ at the steady state. To calculate Δn_{calc} using Eq. (4), one needs to
 356 evaluate four quantities in total: two optical contrast factors, concentration and
 357 temperature differences along the cell's height. The concentration difference
 358 is estimated directly, because the concentration at the interface is determined
 359 by the saturated vapor pressure, while it is zero at the top of the air-purged
 360 cell, $\Delta x_v = x_v^\circ - 0 = p_s/p$. Here p_s is the saturation vapor pressure, with
 361 its temperature dependence available in literature for both liquids [39, 38], and
 362 $p = 101\,325$ Pa is the ambient pressure. Both the saturation vapor pressure
 363 p_s and corresponding vapor concentration x_v° are tabulated for all the tested
 364 temperatures in the Supplementary Material. The temperature drop was inves-
 365 tigated in the section above, and the only remaining unknowns in Eq. (4) are
 366 the contrast factors.

The Lorentz–Lorenz equation is widely used for the description of a refractive index n of pure transparent substances through their effective molecular polarizability α :

$$\frac{n^2 - 1}{n^2 + 2} = \frac{4\pi}{3} N\alpha, \quad \text{or,} \quad \frac{n^2 - 1}{n^2 + 2} = \frac{4\pi}{3} \frac{\rho N_A}{M} \alpha, \quad (5)$$

where N is the number of molecules of the substance per unit volume, $N_A = 6.022 \times 10^{23} \text{ mol}^{-1}$ is the Avogadro constant, ρ is the density (mass per unit volume), and M is the molar mass. When the polarisability is small and the square of the refractive index is $n^2 \approx 1$, which holds for many gases, Eq. (5) reduces to:

$$n^2 - 1 \approx 4\pi N\alpha$$

or, under condition of $n + 1 \approx 2$, it turns into the Gladstone–Dale expression:

$$n - 1 \approx 2\pi N\alpha = 2\pi \frac{\rho N_A}{M} \alpha. \quad (6)$$

To obtain the concentration dependence of the refractive index, Eqs. (5) and (6) can be extended for mixtures by assuming a linear additive rule for the polarizability [40, 41]

$$n - 1 = 2\pi N_A \rho_t \sum_{i=1}^n \frac{w_i \alpha_i}{M_i}, \quad (7)$$

where w_i , M_i , and α_i are the mass fraction, the molar mass, and the molecular polarizability of component i , respectively, and ρ_t is the mass density of the mixture. Converting the concentration into mole fractions x_i , the expression now takes the following form:

$$n - 1 = 2\pi N_A c_t \sum_{i=1}^n x_i \alpha_i, \quad (8)$$

where c_t is the molar density of the mixture (mol/m^3) defined as

$$c_t = \frac{p}{RT} \quad (9)$$

where p is the total (here atmospheric) pressure (Pa), T is the absolute temperature (K), and $R = 8.314463 \text{ m}^3 \text{ Pa K}^{-1} \text{ mol}^{-1}$ is the gas constant. Finally, the formula for the refractive index of the vapour-air mixture is

$$n = 1 + 2\pi N_A \frac{p}{RT} [\alpha_a + x_v(\alpha_v - \alpha_a)] , \quad (10)$$

368 where the subscript 'a' corresponds to air and the subscript 'v' to vapour.

369 3.3.2. Optical contrast factors

The optical contrast factors are calculated taking the derivatives of Eq. (10), as shown in the Supplementary Material. We found that the thermal contribution into the entire Δn_{calc} , the second term in Eq. (4), is small and varies in the range from 1.1 to 3.5% of the concentration part. This finding allows us to safely neglect the temperature input into the refractive index (second term in RHS of Eq. (4)), and to estimate of the concentration contrast factor directly from the experiment, as

$$\left(\frac{\partial n}{\partial x} \right)_{exp} = \frac{\Delta n_{exp}}{x_v^o} \quad (11)$$

370 Both, calculated Δn_{calc} and experimental Δn_{exp} are presented in Fig. 7 and
371 their values are given in Table S3 of Supplementary Material.

372 Figure 7 shows that a theoretical approach to evaluate the contrast factors
373 of vapor-air mixtures works very well at room temperature and above, while at
374 lower temperatures, the agreement with experiment is less good. The difference
375 between the theoretical and experimental values is temperature-dependent and
376 varies between 0 to 20% approximately. For all the temperatures, the ratio of
377 the experimental and calculated values is of the same order for both liquids.

378 Another important result is the demonstrated consistency of our measure-
379 ments with the available literature data on the molecular polarizability of pure
380 substances, their saturation vapor pressure, and other thermophysical proper-
381 ties. This consistency justifies using of the experimentally determined concen-
382 tration contrast factors in the next part of the paper, when needed.

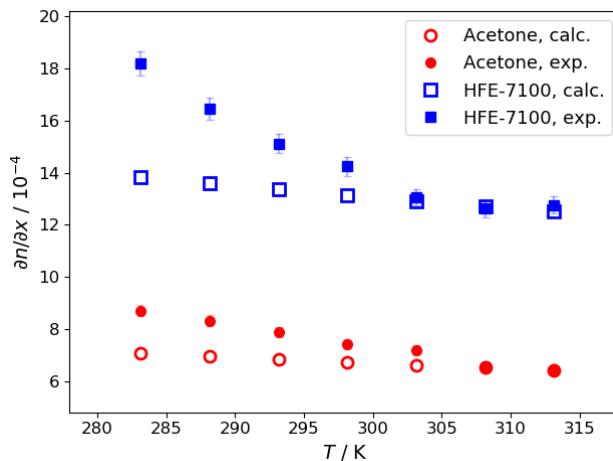


Figure 7: Calculated and measured optical concentration-related contrast factor ($\partial n/\partial x$) for the vapor-air mixture of acetone and HFE-7100 over examined temperature range.

383 3.4. Diffusion coefficients of vapors in air

384 3.4.1. Governing equations

385 The diffusion problem is treated using the so-called “diffusion through a
386 stagnant gas film” model which is a well described in [42]. In the frame of
387 this model, the evaporating substance is moving up (diffusing) through a gas
388 “film” (i.e., a gas layer) which is stagnant (not moving). At steady state, the
389 air flux in the diffusion tube is absent (provided that the solubility of air in the
390 liquid is negligible). We consider this assumption perfectly valid in our case,
391 as we always used non-degassed liquid in experiments, and the tiny amount of
392 the liquid sample does additionally guarantee an absence of any measurable air
393 dissolution in the liquid.

The total flux of diffusing vapor, N_v , consists of convective and diffusive parts, as

$$N_v = x_v(N_v + N_a) - cD\frac{\partial x_v}{\partial z} \quad (12)$$

where x_v is the vapor concentration in mole fractions; N_v and N_a are the vapor and air fluxes, respectively, ($\text{mol s}^{-1} \text{ m}^{-2}$); c is the total molar concentration of the gas, (mol m^{-3}) and D is the vapor diffusion coefficient ($\text{m}^2 \text{ s}^{-1}$). In the

ideal gas approximation, the total concentration c is given by Eq. (9). Since the air is stagnant (i.e., $N_a = 0$), Eq. (12) turns into

$$N_v(z) = -\frac{cD}{1-x_v} \frac{\partial x_v}{\partial z} \quad (13)$$

When the system reaches a steady state, with no concentration change in time, the spatially-invariant vapor flux can be written as

$$-\frac{dN_v(z)}{dz} = 0 \quad \rightarrow \quad \frac{d}{dz} \left(\frac{cD}{1-x_v} \frac{dx_v}{dz} \right) = 0 \quad (14)$$

With general boundary conditions, $x_{v1} = x_v(z_1)$ and $x_{v2} = x_v(z_2)$, the solution of Eq. (14) takes form (for details see in [42]):

$$\left(\frac{1-x_v(z)}{1-x_{v1}} \right) = \left(\frac{1-x_{v2}}{1-x_{v1}} \right)^{\frac{z-z_1}{z_2-z_1}} \quad (15)$$

In our case, with zero vapor concentration at the top of the cell, $x_{v2} = 0$ at $z_2 = H$, and the saturation concentration at the interface, $x_{v1} = x_v^\circ$ at $z_1 = b$, the solution is reduced to

$$x_v(z) = 1 - (1-x_v^\circ)^{\frac{H-z}{H-b}} \quad (16)$$

Using Eq. (16) one can find an explicit expression for the derivative $\frac{\partial x_v}{\partial z} \Big|_{z=b}$, to substitute in Eq. (13). This leads to an expression bounding the diffusion coefficient with the evaporation rate N_v° and the thickness of the stagnant gas layer ($H-b$) as

$$N_v^\circ = \frac{cD}{H-b} \ln \left(\frac{1}{1-x_v^\circ} \right) \quad (17)$$

The vapor concentration at the interface, x_v° , can be derived from the saturation vapor pressure p_s at a given temperature as $x_v^\circ = p_s/p$. The working equations for p_s are available in the literature for a wide range of liquids, and for acetone it is given by the Antoine equation [39]

$$\log_{10}(p_s[\text{bar}]) = 4.4245 - \left(\frac{1312.25}{T[\text{K}] - 32.45} \right) \quad (18)$$

and for HFE-7100 by equation [38] :

$$\ln(p_s[\text{Pa}]) = 22.415 - \left(\frac{3641.9}{T[\text{K}]} \right) \quad (19)$$

394 The saturation vapor pressure for acetone and HFE-7100 is tabulated in
395 Table S3 of Supplementary Material, and the corresponding vapor concentration
396 (in molar fractions) is given in section 3.4.3, see Table 3.

397 It is worth mentioning also that the interfacial evaporation rate N_v° is equiv-
398 alent to the time-averaged evaporation rate N_v , see Eq. (3) in section 3.2.1.
399 The latter one was measured as a global rate in a steady state, but due to 1D
400 character of the problem and the invariance of the vapor flux along z -axis (cf.
401 Eq. (14)), it is equivalent to the former.

402 Recall that Eq. (17) is obtained under condition of the motionless interface.
403 An alternative expression that considers the movement of the interface due to
404 evaporation does exist as well [42], and it requires monitoring of the interface
405 position with time [27]. In our experiments, the liquid layer was intentionally
406 chosen to be small compared to the total cell height, $b \ll H$, so that the interface
407 motion can be neglected.

408 In total, four quantities are needed to calculate the diffusion coefficient out
409 of Eq. (17). Among them three quantities were determined above: the gas
410 concentration c , the saturation vapor concentration x_v° , the evaporation rate
411 N_v° . The remaining quantity is the diffusion path length. One may assume that
412 the vapor diffusion path is fixed by the cell geometry and is equal to $H - b$.
413 However, this approach may lead to an essential error in the diffusion coefficient
414 which is discussed in the next section.

415 3.4.2. *Experimental concentration profiles and diffusion path length*

416 The observed profiles of the vapor concentration inside the diffusion tube
417 are expected to closely follow their theoretical shape, outlined by Eq. (16). We
418 have found, however, that in all conducted experiments it was never the case.

419 One of the typical situations is illustrated in Fig. 8. The solid curve presents
420 the experimental results obtained in regime II, when the refractive index is
421 converted to concentration. Accordingly, the shape of the curve is similar to
422 that one in Fig. 5, but taken for another temperature. The dash-dotted curve
423 is the theoretical curve according to Eq. (16) where x_v° is the saturation va-

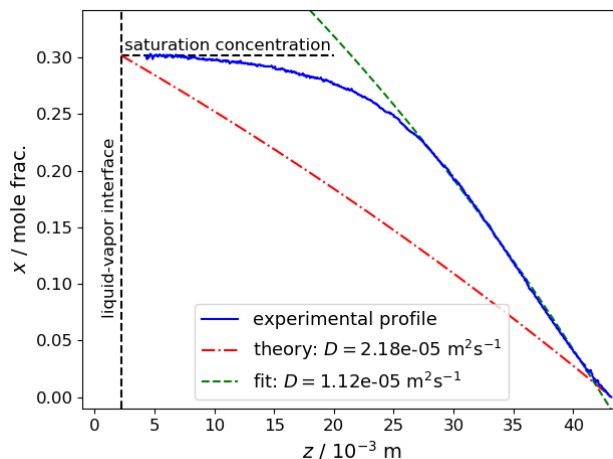


Figure 8: The distribution of vapor concentration along the cell obtained with different raw approaches: the experimental curve (solid), the theoretical curve according to Eq. (16) (dash-dotted) and the curve obtained by fitting (dashed).

424 por pressure, and H and b are taken from the experiment after filling the cell.
 425 This theoretical curve connects the two pivot points of the system: the satu-
 426 rated vapor concentration at the liquid-vapor interface and the vanishing vapor
 427 concentration at the top of the cell. Obviously, apart from these two points,
 428 this curve has nothing more in common with the actual vapor concentration in
 429 the tube. Furthermore, the diffusion coefficient obtained from this curve (and
 430 shown in the legend) is twice that of the literature data. At the same time, we
 431 have noticed that there exists an extended region with the constant slope on
 432 the experimental profile. Targeting only this part of the experimental profile,
 433 we limited the region $z_1 < z < z_2$ (e.g., $z_1=25$ mm and $z_2=41$ mm) and fitted
 434 Eq. (15) to the experimental data using x_v^o as the fit parameter. The results of
 435 this fit (shown by the dashed curve) are in line with the experiment and provide
 436 a reasonable value for the diffusion coefficient.

437 Figure 8 evidences that the experimental curve may be divided into regions,
 438 where it either coincides with the analytical solution or deviates from it. Thus,
 439 the next task is to identify perturbed regions and determine the cause of their

440 occurrence. Comparison of the experimental and fitting curves shows visible
441 deviations at two extremes. A tiny divergence occurs at the very top of the cell,
442 $41 < z < 43$ mm, and a noticeable deviation occurs in the lower part of the cell,
443 $z < 25$ mm.

444 The reason for the disturbance at the top of the diffusion cell is fairly easy to
445 identify, it is caused by the air flow around the cell, as discussed in Sec. 2. The
446 air flow may partly propagate into the cell volume causing deformation of the
447 concentration profile at the very top. The deviation near the bottom is much
448 stronger and the reason is not so obvious.

449 Upon closer examination of Fig. 8 it can be seen that the vapor concentration
450 changes only slightly within the lower third of the cell height. This observation
451 contradicts the assumed diffusive transport in the region, and can be explained
452 by mixing due to convection in the gas, even if rather slow. Identifying a
453 possible source of convection in the gas does not pose a problem, since it can
454 be triggered by Marangoni convection at the liquid interface. As demonstrated
455 in section 3.2.2 and in Supplementary Material, evaporation causes a small, but
456 not negligible drop in temperature at the interface. Due to imperfect boundary
457 conditions at the lateral walls, this thermal effect can be non-uniform along the
458 interface, resulting in Marangoni flows strong enough to drive the gas motion.

459 The used digital interferometry enables the tracing the evolution of the con-
460 centration field in time in the entire 2D region. Figure 9a shows distribution of
461 the wrapped phase in a typical image. It is clearly seen that in the upper half
462 of the cell, the isolines of the wrapped phase are horizontal, which evidences
463 1D mass transfer in the region. In contrast, the isolines in the lower part are
464 concave towards the interface, which confirms the hypothesis of the presence of
465 convection in the region. It is worth noting that such phase maps were rather
466 common in experiments, especially in the case of acetone.

467 Summing up the above considerations, along the experimental cell, we have
468 identified three regions with different transport mechanisms which are depicted
469 in Fig. 9b. The self-explanatory sketch demonstrates that the pure diffusive
470 mechanism takes place only in the limited part of the cell, which is completely

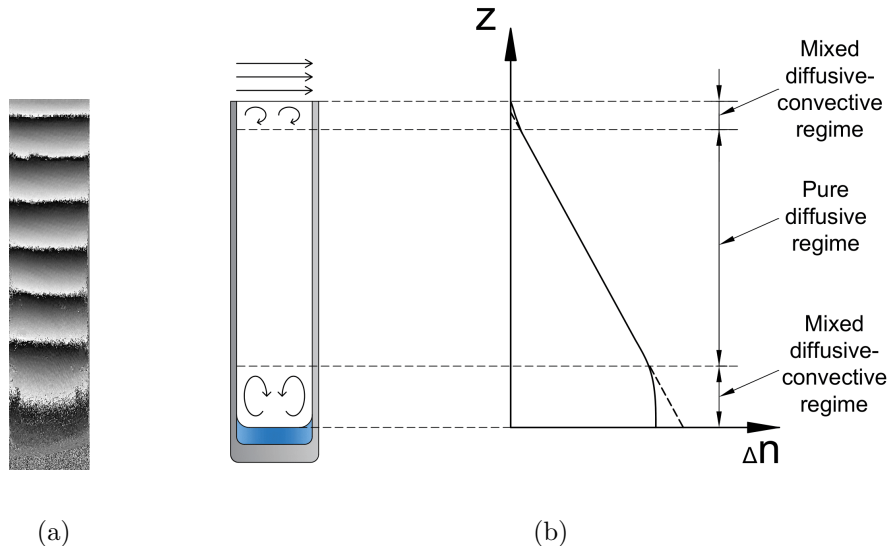


Figure 9: (a) Wrapped optical phase map corresponding to evaporation of acetone at $T = 308.15$ K. (b) Revealed mechanisms of vapor transfer through the cell.

471 free of convective disturbances of various origins. This calls for a specific adap-
 472 tation of the data extraction procedure.

473 Two ways can be suggested to overcome this problem. The first one, already
 474 implemented for the dashed curve in Fig. 8, uses the limiting concentrations
 475 x_v^o as free fit parameter. This approach is somewhat artificial, and results in
 476 arbitrary values of the limiting vapor concentrations at the interface and the
 477 cell's top. In what follows, we omit this approach.

478 The second option retains the correct limiting concentrations, but requires
 479 an estimate of the “true” (or effective) diffusion path in the system as illustrated
 480 in Fig. 10. Regions prone to convection are cropped out and the stagnant gas
 481 layer is considered true over distance L_{eff} . Then the experimental data are fitted
 482 to the analytical solution only in this layer. For this, the initial thickness of the
 483 gas layer ($H - b$) should be replaced by its effective analogue L_{eff} in Eq. (17).

484 Next, we determined the effective diffusion path in all the conducted ex-
 485 periments, and these data are presented by symbols in Fig. 11. Interestingly,

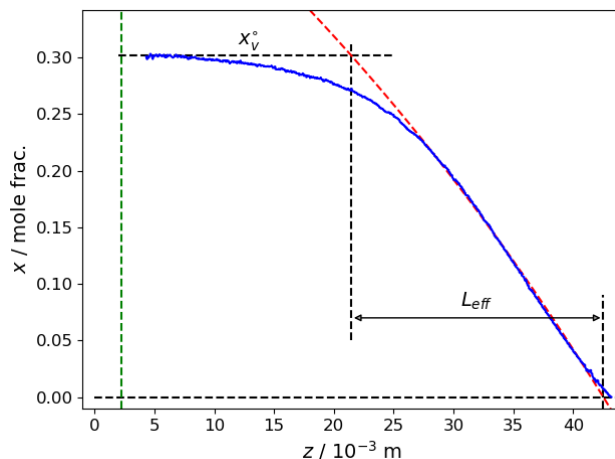


Figure 10: Determination of the cell length (L_{eff}) where the diffusive transport mechanism occurs. The large region in the lower part is presumably affected by Marangoni convection. The tiny region at the top is perturbed by the ambient air flow.

486 the effective diffusion path increases with temperature, which means that the
 487 region adjacent to the interface and disturbed by convection does contract with
 488 increasing temperature. This contraction is especially noticeable in the case of
 489 acetone.

490 The data of the effective diffusion path is used to determine the diffusion
 491 coefficient and, looking at the possible trend curves in Fig. 11, we see that they
 492 are slightly scattered. So, we search a polynomial interpolation of the obtained
 493 L_{eff} and further use the L_{eff} value from this polynomial, rather than the one
 494 directly obtained from the experiment.

495 We have interpolated the data on L_{eff} by power series polynomials of the
 496 lowest possible order so that the interpolation curve remains within the mea-
 497 surement error. A careful estimate of the corresponding error-bars for acetone is
 498 10%, which limits the polynomial power to quadratic. In the case of HFE-7100
 499 the error-bar is much smaller, 1.8% only, which requires the polynomial of third
 500 order to fit. We do not provide these polynomials explicitly as they do not have
 501 a special value, but the values of interpolated L_{eff} , used for calculation of the

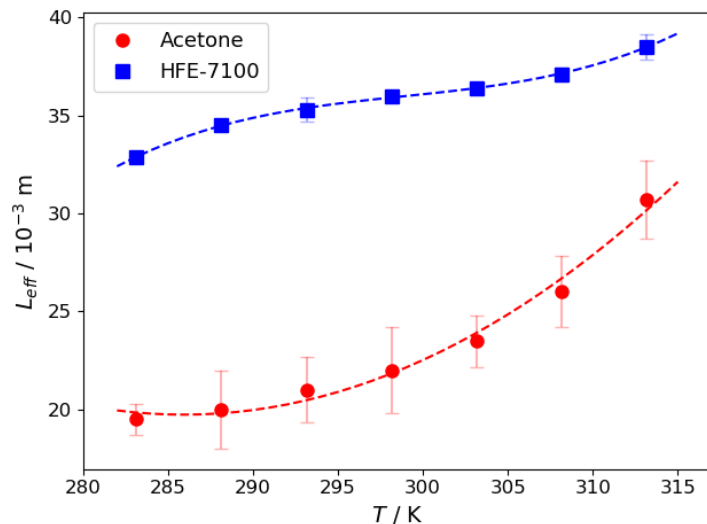


Figure 11: Temperature dependence of the effective diffusion length L_{eff} . The symbols indicate points obtained from fitting of experimental results, and the dashed curves represent the polynomial interpolation: the second order for acetone and the third order for HFE-7100. The interpolated values will be used to determine the vapor diffusion coefficients of acetone and HFE-7100 in air. The error bars are standard deviations.

502 diffusion coefficients, are given in Table 3.

503 3.4.3. Diffusion coefficients

504 At this point, all the quantities required to calculate the diffusion coefficient
 505 using Eq. (17) have been determined, they are x_v° , N_v° , L_{eff} . Before placing
 506 them in the final table, they were approximated by power polynomials in order to
 507 reduce the possible scattering of the resulting diffusion coefficients. For example,
 508 the evaporation rate N_v° was not taken from Table 2, instead, it was calculated
 509 by interpolation polynomials Eq. (3). Similarly, the effective diffusion length
 510 was not taken from experimental points in Fig. 11, but from the interpolation
 511 curves shown there. All these improved data are summarised in Table 3.

512 Since we care about the quality of the initial data, the correct estimation of
 513 the net error of the diffusion coefficient is important. Among the three param-

Table 3: Saturation vapor concentration $x_v^\circ/\text{mol mol}^{-1}$, evaporation rate $N_v^\circ/10^{-3}\text{ mol s}^{-1}\text{ m}^{-2}$, effective diffusion path $L_{\text{eff}}/10^{-3}\text{ m}$, and vapor-in-air diffusion coefficient $D/10^{-5}\text{ m}^2\text{ s}^{-1}$ of acetone and HFE-7100 at different temperatures T/K .

T	x_v°	N_v°	L_{eff}	D
<i>Acetone</i>				
283.15	0.1529	3.46	19.8	0.96
288.15	0.1936	4.69	19.8	1.02
293.15	0.2428	6.08	20.4	1.07
298.15	0.3020	7.64	21.8	1.13
303.15	0.3726	9.36	23.9	1.19
308.15	0.4562	11.3	26.6	1.24
313.15	0.5545	13.3	30.1	1.27
<i>HFE-7100</i>				
283.15	0.1390	1.10	32.9	0.56
288.15	0.1738	1.29	34.5	0.55
293.15	0.2156	1.60	35.4	0.56
298.15	0.2655	2.03	35.9	0.58
303.15	0.3248	2.58	36.4	0.59
308.15	0.3947	3.25	37.1	0.61
313.15	0.4766	4.04	38.5	0.62

514 eters that contribute to the final error, we will consider two, N_v° and L_{eff} , as
515 they are the main contributors. As stated above, the largest relative error in the
516 evaporation rate N_v° is 7% for HFE-7100 and 12% for acetone. For the effective
517 diffusion length L_{eff} , the largest relative error is only 1.8% for HFE-7100 and
518 10% for acetone. We emphasize, that the above errors are the largest among the
519 measurements performed in the temperature range from 283.15 K to 313/15 K.
520 The relative error of D is calculated as the square root of the relative errors

521 squared of the contributing terms. This evaluation provides the largest relative
522 error for diffusion D which is 7.2% for HFE-7100 and 15.6% for acetone.

523 The determined diffusion coefficients, together with the error-bars and trend-
524 lines, are shown in Fig. 12, and compared with available literature data. For
525 acetone, the present results agree well within the error bar with the measure-
526 ments reported in [43, 44, 45, 46] and demonstrate very good agreement with
527 interpolation presented in [8]. For HFE-7100 we presented only our original
528 data.

To parameterize the temperature dependency of the diffusion coefficients,
we have fitted them to a kind of the Arrhenius equation

$$D(T) = D_0 \exp\left(-\frac{E_a}{RT}\right) \quad (20)$$

529 where D_0 is a coefficient, and E_a is a so-called activation energy of the process.
530 This fit agrees well with our data, and can be seen as the dashed curves on both
531 panels of Fig. 12.

532 The numeric values of the fit parameters are:

533 $D_0 = 2.963 \cdot 10^{-5} \text{ m}^2 \text{ s}^{-1}$ and $E_a = 7055 \text{ J mol}^{-1}$ (for acetone),

534 $D_0 = 1.016 \cdot 10^{-5} \text{ m}^2 \text{ s}^{-1}$ and $E_a = 3882 \text{ J mol}^{-1}$ (for HFE-7100).

535 4. Conclusions

536 In this work, we demonstrate the broad capabilities of optical digital inter-
537 ferometry for measuring the evaporation rate and determining diffusion coeffi-
538 cients, optical contrast coefficients, and temperature drop on the evaporative
539 interface of vapour-air mixtures. The stabilized Mach-Zehnder interferometer
540 with modern phase extraction algorithm allows the tracing of the vapour dis-
541 tribution in the entire two-dimensional cross-section of the cell, both in steady-
542 state and transient regimes. Our findings are based on complete evaporation of
543 a thin liquid layer from a rectangular cuvette with an open end. Evaporation of
544 strongly volatile (acetone) and moderately volatile (HFE-7100) liquids into air
545 was investigated in the temperature range from 283.15 to 313.15 K.

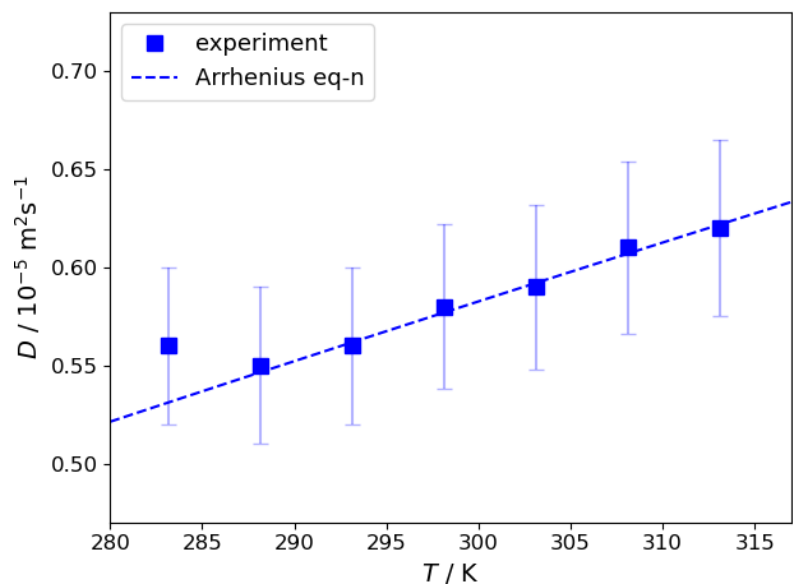
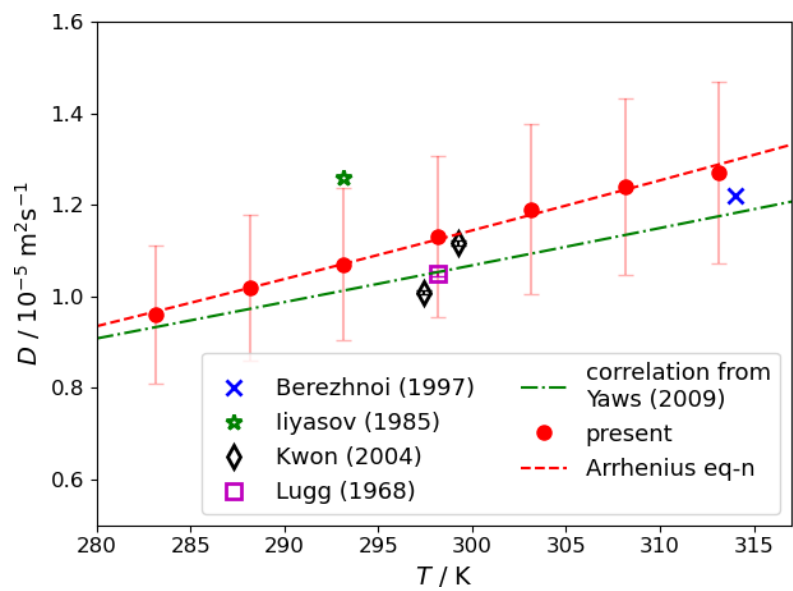


Figure 12: Diffusion coefficient of acetone vapor-in-air (top). Comparison of present measurements with literature data at different temperatures. Diffusion coefficient of HFE-7100 vapor-in-air (bottom)

546 Tracing the evolution of the refractive index, three different temporal regimes
547 of vapour diffusion were identified occurring at different times of the experiment,
548 and among them the longest one corresponds to the steady evaporation. The
549 evaporation rate, as well as the evaporative heat flux, was determined by optical
550 measurements of the evaporation time in the steady regime.

551 The temperature drop evaluation at the interface revealed that the temper-
552 ature variation inside the cell is weak enough to neglect its contribution to the
553 refractive index variation, but strong enough to cause Marangoni convection at
554 the interface. The 2D maps of the optical phase clearly showed that the dif-
555 fusion process was disrupted at both ends of the tube. Near the interface, the
556 Marangoni convection, although weak, remixes vapour and air while near the
557 open end the external air flow partly propagates into the cell volume. Thanks to
558 interferometric 2D images, regions with disturbed diffusion regime were localised
559 and excluded from consideration, so that a true diffusion path was determined
560 in each experiment.

561 The diffusion coefficients of vapour in air were determined using a working
562 equation based on the “diffusion through a stagnant gas film” model and on
563 the true diffusion path. A good agreement of the measured diffusion coefficients
564 with available literature data for acetone validates the interferometric approach
565 we developed in this work.

566 The instrument we designed and built, together with the novel experimental
567 procedure we implemented, made it possible to quickly and reliably gain access
568 to important properties of vapour-air mixtures, such as the diffusion coefficient
569 and optical contrast factors in particular. We may therefore conclude that in-
570 terferometric measurements open new promising perspectives for better control
571 of diffusion of vapour in gases.

572 **CRedit authorship contribution statement**

573 **V. Shevchenko:** Data Curation, Investigation. **A. Mialdun:** Methodol-
574 ogy, Software, Writing - Original Draft. **V. Yasnou:** Investigation, Validation.

575 **Y. V. Lyulin:** Formal analysis, Writing - Original Draft **H. Ouerdane:** Su-
576 pervision, Writing - Review & Editing. **V. Shevtsova:** Conceptualization,
577 Supervision, Writing - Review & Editing.

578 **Declaration of Competing Interest**

579 The authors declare that they have no known competing financial interests or
580 personal relationships that could have appeared to influence the work reported
581 in this paper.

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